## TEST PAPER OF JEE(MAIN) EXAMINATION – 2019 (Held On Thursday 10<sup>th</sup> JANUARY, 2019) TIME : 02 : 30 PM To 05 : 30 PM PHYSICS

1. Two forces P and Q of magnitude 2F and 3F, respectively, are at an angle  $\theta$  with each other. If the force Q is doubled, then their resultant also gets doubled. Then, the angle is : (1) 30° (2) 60° (3) 90° (4) 120°

### Ans. (4)

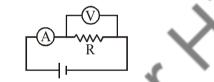
Sol.  $4F^2 + 9F^2 + 12F^2 \cos \theta = R^2$   $4F^2 + 36 F^2 + 24 F^2 \cos \theta = 4R^2$   $4F^2 + 36 F^2 + 24 F^2 \cos \theta$  $= 4(13F^2 + 12F^2\cos\theta) = 52 F^2 + 48F^2\cos\theta$ 

$$\cos \theta = -\frac{12F^2}{24F^2} = -\frac{1}{2}$$

2. The actual value of resistance R, shown in the figure is  $30\Omega$ . This is measured in an experiment as shown using the standard

formula  $R = \frac{V}{I}$ , where V and I are the readings

of the voltmeter and ammeter, respectively. If the measured value of R is 5% less, then the internal resistance of the voltmeter is :



(1)  $350\Omega$  (2)  $570\Omega$  (3)  $35 \Omega$  (4)  $600 \Omega$ Ans. (2)

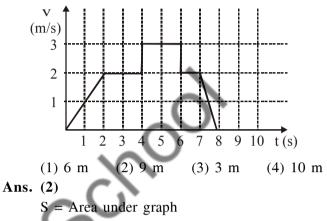
- Sol. 0.95 R =  $\frac{R R_{\upsilon}}{R + R_{\upsilon}}$ 0.95 × 30 = 0.05 R<sub>v</sub> R<sub>v</sub> = 19 × 30 = 570 Ω
- 3. An unknown metal of mass 192 g heated to a temperature of 100°C was immersed into a brass calorimeter of mass 128 g containing 240 g of water a temperature of 8.4°C Calculate the specific heat of the unknown metal if water temperature stabilizes at 21.5°C (Specific heat of brass is 394 J kg<sup>-1</sup> K<sup>-1</sup>)

(3) 
$$654 \text{ J kg}^{-1} \text{ K}^{-1}$$
 (4)  $916 \text{ J kg}^{-1} \text{ K}^{-1}$ 

Ans. (4)

Sol. 
$$192 \times S \times (100 - 21.5)$$
  
=  $128 \times 394 \times (21.5 - 8.4)$   
+  $240 \times 4200 \times (21.5 - 8.4)$   
 $\Rightarrow S = 916$ 

4. A particle starts from the origin at time t = 0 and moves along the positive x-axis. The graph of velocity with respect to time is shown in figure. What is the position of the particle at time t = 5s?



$$x 2 x 2 + 2 x 2 + 3 x 1 = 9$$

The self induced emf of a coil is 25 volts. When the current in it is changed at uniform rate from 10 A to 25 A in 1s, the change in the energy of the inductance is :

m

Ans. (1)

2

5.

$$L\frac{di}{dt} = 25$$
$$L \times \frac{15}{1} = 25$$
$$L = \frac{5}{3}H$$

$$\Delta E = \frac{1}{2} \times \frac{5}{3} \times (25^2 - 10^2) = \frac{5}{6} \times 525 = 437.5 \text{ J}$$

6. A current of 2 mA was passed through an unknown resistor which dissipated a power of 4.4 W. Dissipated power when an ideal power supply of 11V is connected across it is :

(1) $11 \times 10^{-5} \text{ W}$	(2) $11 \times 10^{-4} \text{ W}$
(3) $11 \times 10^5$ W	(4) $11 \times 10^{-3}$ W

1

Ans. (1)  $P = I^{2}R$   $4.4 = 4 \times 10^{-6} R$   $R = 1.1 \times 10^{6} \Omega$   $P' = \frac{11^{2}}{R} = \frac{11^{2}}{1.1} \times 10^{-6} = 11 \times 10^{-5} W$ 

7. The diameter and height of a cylinder are measured by a meter scale to be  $12.6 \pm 0.1$  cm and  $34.2 \pm 0.1$  cm, respectively. What will be the value of its volume in appropriate significant figures ?

(1) 
$$4260 \pm 80 \text{ cm}^3$$
 (2)  $4300 \pm 80 \text{ cm}^3$ 

(3) 
$$4264.4 \pm 81.0 \text{ cm}^3$$
 (4)  $4264 \pm 81 \text{ cm}^3$ 

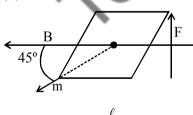
$$V = \pi \frac{d^2}{4} h = 4260 \text{ cm}^3$$
  
$$\frac{\Delta V}{V} = \frac{2\Delta d}{d} + \frac{\Delta h}{h}$$
  
$$\frac{\Delta V}{V} = 2 \times \frac{0.1V}{12.6} + \frac{0.1V}{34.2}$$
  
$$= \frac{0.2}{12.6} \times 4260 + \frac{0.1 \times 4260}{34.2} = 80$$

8. At some location on earth the horizontal component of earth's magnetic field is  $18 \times 10^{-6}$  T. At this location, magnetic neeedle of length 0.12 m and pole strength 1.8 Am is suspended from its mid-point using a thread, it makes 45° angle with horizontal in equilibrium. To keep this needle horizontal, the vertical force that should be applied at one of its ends is :

(1) 
$$3.6 \times 10^{-5}$$
 N (2)  $6.5 \times 10^{-5}$  N  
(3)  $1.3 \times 10^{-5}$  N (4)  $1.8 \times 10^{-5}$  N

Ans. (2)

2



mBl sin 45<sup>0</sup> = 
$$F\frac{2}{2}$$
 sin 45<sup>0</sup>  
F = 2mB = 3.6×18×10<sup>-6</sup>  
= 6.5×10<sup>-5</sup> N

**9.** The modulation frequency of an AM radio station is 250 kHz, which is 10% of the carrier wave. If another AM station approaches you for license what broadcast frequency will you allot ?

(1) 2750 kHz	(2) 2000 kHz
(3) 2250 kHz	(4) 2900 kHz

Ans. (2)

$$f_{carrier} = \frac{250}{0.1} = 2500 \text{ KHZ}$$

:. Range of signal = 2250 Hz to 2750 Hz Now check all options : for 2000 KHZ  $f_{mod}$  = 200 Hz

 $\therefore$  Range = 1800 KHZ to 2200 KHZ

10. A hoop and a solid cylinder of same mass and radius are made of a permanent magnetic material with their magnetic moment parallel to their respective axes. But the magnetic moment of hoop is twice of solid cylinder. They are placed in a uniform magnetic field in such a manner that their magnetic moments make a small angle with the field. If the oscillation periods of hoop and cylinder are  $T_h$  and  $T_c$  respectively, then :

(1) 
$$T_h = 0.5 T_c$$
 (2)  $T_h = 2 T_c$   
(3)  $T_h = 1.5 T_c$  (4)  $T_h = T_c$ 

Ans. (4)

$$T = 2\pi \sqrt{\frac{I}{\mu B}}$$
$$T_{h} = 2\pi \sqrt{\frac{mR^{2}}{(2\mu)B}}$$
$$T_{C} = 2\pi \sqrt{\frac{1/2mR^{2}}{\mu B}}$$

11. The electric field of a plane polarized electromagnetic wave in free space at time t= 0 is given by an expression

$$\vec{E}(x,y) = 10\hat{j} \cos [(6x + 8z)]$$

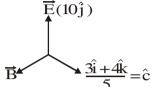
The magnetic field  $\vec{B}$  (x, z, t) is given by : (c is the velocity of light)

(1)  $\frac{1}{c} (6\hat{k} + 8\hat{i}) \cos[(6x - 8z + 10ct)]$ (2)  $\frac{1}{c} (6\hat{k} - 8\hat{i}) \cos[(6x + 8z - 10ct)]$ (3)  $\frac{1}{c} (6\hat{k} + 8\hat{i}) \cos[(6x + 8z - 10ct)]$ (4)  $\frac{1}{c} (6\hat{k} - 8\hat{i}) \cos[(6x + 8z + 10ct)]$  Ans. (2)

 $\vec{E} = 10\hat{j}\cos\left[\left(6\hat{i} + 8\hat{k}\right) \cdot \left(x\hat{i} + z\hat{k}\right)\right]$ 

 $= 10\hat{j}\cos[\vec{K}\cdot\vec{r}]$ 

 $\vec{K} = 6\hat{i} + 8\hat{k}; \text{ direction of waves travel.}$ i.e. direction of 'c'.



 $\therefore$  Direction of  $\hat{B}$  will be along

$$\hat{C} \times \hat{E} = \frac{-4i + 3k}{5}$$

Mag. of  $\vec{B}$  will be along  $\hat{C} \times \hat{E} = \frac{-4\hat{i} + 3\hat{k}}{5}$ 

Mag. of 
$$\vec{B} = \frac{E}{C} = \frac{10}{C}$$
  
$$\therefore \quad \vec{B} = \frac{10}{C} \left( \frac{-4\hat{i} + 3\hat{k}}{5} \right) = \frac{\left(-8\hat{i} + 6\hat{k}\right)}{C}$$

12. Condiser the nuclear fission  $Ne^{20} \rightarrow 2He^4 + C^{12}$ 

Given that the binding energy/nucleon of  $Ne^{20}$ , He<sup>4</sup> and C<sup>12</sup> are, respectively, 8.03 MeV, 7.07 MeV and 7.86 MeV, identify the correct statement :

- (1) 8.3 MeV energy will be released
- (2) energy of 12.4 MeV will be supplied
- (3) energy of 11.9 MeV has to be supplied
- (4) energy of 3.6 MeV will be released

### Ans. (3)

 $\begin{array}{rcl} \text{Ne}^{20} & \rightarrow & 2\text{He}^4 + \text{C}^{12} \\ \text{8.03} \times 20 & & 2 \times 7.07 \times 4 + 7.86 \times 12 \\ \therefore & \text{E}_{\text{B}} = (\text{BE})_{\text{react}} & - (\text{BE})_{\text{product}} = 9.72 \text{ MeV} \end{array}$ 

13. Two vectors  $\vec{A}$  and  $\vec{B}$  have equal magnitudes. The magnitude of  $(\vec{A} + \vec{B})$  is 'n' times the magnitude of  $(\vec{A} - \vec{B})$ . The angle between  $\vec{A}$  and  $\vec{B}$  is :

(1) 
$$\sin^{-1}\left[\frac{n^2-1}{n^2+1}\right]$$
 (2)  $\cos^{-1}\left[\frac{n-1}{n+1}\right]$   
(3)  $\cos^{-1}\left[\frac{n^2-1}{n^2+1}\right]$  (4)  $\sin^{-1}\left[\frac{n-1}{n+1}\right]$ 

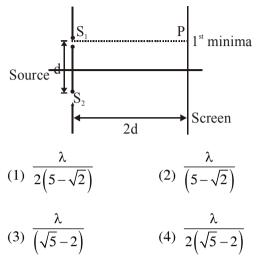
Ans. (3)

A particle executes simple harmonic motion with an amplitude of 5 cm. When the particle is at 4 cm from the mean position, the magnitude of its velocity in SI units is equal to that of its acceleration. Then, its periodic time in seconds is :

(1) $\frac{7}{3}\pi$	(2) $\frac{3}{8}\pi$
$(3) \ \frac{4\pi}{3}$	$(4) \ \frac{8\pi}{3}$

Ans. (4)

15. Consider a Young's double slit experiment as shown in figure. What should be the slit separation d in terms of wavelength  $\lambda$  such that the first minima occurs directly in front of the slit (S<sub>1</sub>) ?



Ans. (4)

- $\sqrt{5}d 2d = \frac{\lambda}{2}$
- 16. The eye can be regarded as a single refracting surface . The radius of curvature of this surface is equal to that of cornea (7.8 mm). This surface separates two media of refractive indices 1 and 1.34. Calculate the distance from the refracting surface at which a parallel beam of light will come to focus.

4.0 cm

(3) 3.1 cm

Ans. (3)

$$R = 7.8 \text{ mm}$$

$$\mu = 1 \quad \mu = 1.34$$

$$\frac{1.34}{V} - \frac{1}{\infty} = \frac{1.34 - 1}{7.8}$$

$$\therefore$$
 V = 30.7 mm

Half mole of an ideal monoatomic gas is heated at constant pressure of 1atm from 20 °C to 90°C. Work done by gas is close to : ( Gas constant R = 8.31 J /mol.K)

(1) 73 J (2) 291 J (3) 581 J (4) 146 J Ans. (2)

$$WD = P\Delta V = nR\Delta T = \frac{1}{2} \times 8.31 \times 70$$

18. A metal plate of area  $1 \times 10^{-4}$  m<sup>2</sup> is illuminated by a radiation of intensity 16 mW/m<sup>2</sup>. The work function of the metal is 5eV. The energy of the incident photons is 10 eV and only 10% of it produces photo electrons. The number of emitted photo electrons per second and their maximum energy, respectively, will be :  $[1 \text{ eV} = 1.6 \times 10^{-19}\text{J}]$ 

(1) 
$$10^{10}$$
 and 5 eV (2)  $10^{14}$  and 10 eV

(3)  $10^{12}$  and 5 eV (4)  $10^{11}$  and 5 eV

Ans. (4)

Maximum kinetic energy  $KE_{max} = E - \phi$ 

$$KE_{max} = 10eV - 5eV = 5eV$$

No. of photons incident per unit time  $\frac{n}{t} = \frac{IA}{E}$ 

 $\frac{n}{t} \!=\! \frac{16 \!\times\! 10^{-3} \!\times\! 10^{-4}}{10 \!\times\! 1.6 \!\times\! 10^{-19}} \!=\! 10^{12}$ 

No. of photoelectrons ejected per unit time  $\frac{n}{t} = \frac{10}{100} \times 10^{12} = 10^{11}$ 

19. Charges -q and +q located at A and B, respectively, constitute an electric dipole. Distance AB = 2a, O is the mid point of the dipole and OP is perpendicular to AB. A charge Q is placed at P where OP = y and y >> 2a. The charge Q experiences and electrostatic force F. If Q is now moved along the equatorial line

to P' such that OP'=
$$\left(\frac{y}{3}\right)$$
, the force on Q will be  
close to : $\left(\frac{y}{3} >> 2a\right)$   
P'  
A • - q P'  
O B  
+ q  
(1)  $\frac{F}{3}$  (2) 3F (3) 9F (4) 27F

### Ans. (4)

**Sol.** Electric field of equitorial plane of dipole

$$= -\frac{K\vec{P}}{r^3}$$
  

$$\therefore \text{ At P, F} = -\frac{K\vec{P}}{r^3}Q.$$
  

$$\text{ At P}^1, F^1 = -\frac{K\vec{P}Q}{(r/3)^3} = 27 \text{ F}.$$

- Two stars of masses  $3 \times 10^{31}$  kg each, and at 20. distance  $2 \times 10^{11}$ m rotate in a plane about their common centre of mass O. A meteorite passes through O moving perpendicular to the star's rotation plane. In order to escape from the gravitational field of this double star, the minimum speed that meteorite should have at O is : (Take Gravitational constant  $G = 6.67 \times 10^{-11} \text{ Nm}^2 \text{ kg}^{-2}$ 
  - (1)  $1.4 \times 10^5$  m/s (2) 24 ×10<sup>4</sup> m/s (3)  $3.8 \times 10^4$  m/s (4)  $2.8 \times 10^5$  m/s
- Ans. (4)

By energy convervation between 0 &

$$-\frac{GMm}{r} + \frac{-GMm}{r} + \frac{1}{2}mV^{2} = 0 + 0$$

[M is mass of star m is mass of meteroite)

$$\Rightarrow v = \sqrt{\frac{4GM}{r}} = 2.8 \times 10^5 \text{ m/s}$$

A closed organ pipe has a fundamental 21. frequency of 1.5 kHz. The number of overtones that can be distinctly heard by a person with this organ pipe will be : (Assume that the highest frequency a person can hear is 20,000 Hz)

(1) 7(2) 5 (3) 6Ans. (3)

**Sol.** For closed organ pipe, resonate frequency is odd multiple of fundamental frequency.  $\therefore$  (2n + 1) f<sub>0</sub>  $\leq$  20,000  $(f_0 \text{ is fundamental frequency} = 1.5 \text{ KHz})$ 

 $\therefore$  n = 6

22. A rigid massless rod of length 3l has two masses attached at each end as shown in the figure. The rod is pivoted at point P on the horizontal axis (see figure). When released from initial horizontal position, its instantaneous angular acceleration will be :

$$(1) \frac{g}{2l} \qquad (2) \frac{7g}{3l} \qquad (3) \frac{g}{13l} \qquad (4) \frac{g}{3l}$$

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$$(4) \frac{g}{3l}$$

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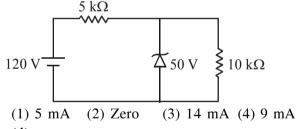
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Ans.

$$\alpha = -\frac{M_0 g \ell}{13M_0 \ell^2} \implies \alpha = -\frac{g}{13\ell}$$

 $\therefore \alpha = \frac{g}{13\ell}$  anticlockwise

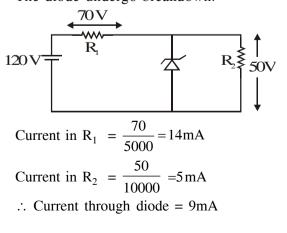
For the circuit shown below, the current through the Zener diode is :



Ans. (4)

(4) 4

Assuming zener diode doesnot undergo breakdown, current in circuit =  $\frac{120}{15000} = 8 \text{ mA}$  $\therefore$  Voltage drop across diode = 80 V > 50 V. The diode undergo breakdown.



Four equal point charges Q each are placed in the xy plane at (0, 2), (4, 2), (4, -2) and (0, -2). The work required to put a fifth charge Q at the origin of the coordinate system will be :

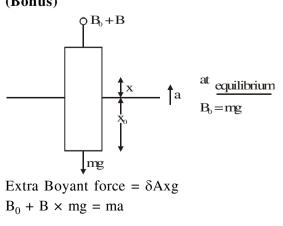
(1) 
$$\frac{Q^2}{2\sqrt{2}\pi\epsilon_0}$$
 (2)  $\frac{Q^2}{4\pi\epsilon_0}\left(1+\frac{1}{\sqrt{5}}\right)$   
(3)  $\frac{Q^2}{4\pi\epsilon_0}\left(1+\frac{1}{\sqrt{3}}\right)$  (4)  $\frac{Q^2}{4\pi\epsilon_0}$ 

Ans. (2)

 $(0.2) \bullet O$ 

Potential at origin =  $\frac{KQ}{2} + \frac{KQ}{2} + \frac{KQ}{\sqrt{20}} + \frac{KQ}{\sqrt{20}}$ (Potential at  $\infty = 0$ )

- = KQ $\left(1 + \frac{1}{\sqrt{5}}\right)$ ∴ Work required to put a fifth charge Q at origin
- is equal to  $\frac{Q^2}{4\pi\epsilon_0}\left(1+\frac{1}{\sqrt{5}}\right)$
- 25. A cylindrical plastic bottle of negligible mass is filled with 310 ml of water and left floating in a pond with still water. If pressed downward slightly and released, it starts performing simple harmonic motion at angular frequency  $\omega$ . If the radius of the bottle is 2.5 cm then  $\omega$  close to : (density of water = 10<sup>3</sup> kg / m<sup>3</sup>) (1) 5.00 rad s<sup>-1</sup> (2) 1.25 rad s<sup>-1</sup>
  - (1) 5.00 rad s<sup>-1</sup> (3) 3.75 rad s<sup>-1</sup>
- (3) 5.75 I Ans. (Bonus)



(4) 2.50 rad s<sup>-1</sup>

$$B = ma$$

$$a = \left(\frac{\delta Ag}{m}\right)^{x}$$

$$w^{2} = \frac{\delta Ag}{m}$$

$$w = \sqrt{\frac{10^{3} \times \pi (2.5)^{2} \times 10^{-4} \times 10}{310 \times 10^{-6} \times 10^{3}}}$$

$$= \sqrt{63.30} = 7.95$$

26. A parallel plate capacitor having capacitance 12 pF is charged by a battery to a potential difference of 10 V between its plates. The charging battery is now disconnected and a porcelain slab of dielectric constant 6.5 is slipped between the plates the work done by the capacitor on the slab is :

$$W = -(U_{f} - U_{i})$$
$$= -\left(\frac{(\varepsilon C)^{2}}{2KC} - \frac{(\varepsilon C)^{2}}{2C}\right)$$
$$= \frac{\varepsilon^{2}C}{2}\left(\frac{K-1}{K}\right)$$
$$= \frac{10^{2} \times 12 \times 10^{-12}}{2}\left(\frac{5.5}{6.5}\right) = 508 \text{pJ}$$

27. Two kg of a monoatomic gas is at a pressure of  $4 \times 10^4$  N/m<sup>2</sup>. The density of the gas is 8 kg /m<sup>3</sup>. What is the order of energy of the gas due to its thermal motion ?

(1) 
$$10^3$$
 J (2)  $10^5$  J  
(3)  $10^6$  J (4)  $10^4$  J

Ans. (4)

Thermal energy of N molecule

$$= N\left(\frac{3}{2}kT\right)$$

$$= \frac{N}{N_A} \frac{3}{2} RT$$

$$= \frac{3}{2} (nRT)$$

$$= \frac{3}{2} PV$$

$$= \frac{3}{2} P\left(\frac{m}{8}\right)$$

$$= \frac{3}{2} \times 4 \times 10^4 \times \frac{2}{8}$$

$$= 1.5 \times 10^4$$
order will 10<sup>4</sup>
A particle which is experiencing a force, given

by  $\vec{F} = 3\vec{i} - 12\vec{j}$ , undergoes a displacement of  $\vec{d} = 4\vec{i}$ . If the particle had a kinetic energy of 3 J at the beginning of the displacement, what is its kinetic energy at the end of the displacement ? (4) 9 J (3) 12 J (1) 15 J (2) 10 J

#### Ans. (1)

28.

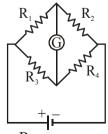
А

Work done =  $\vec{F} \cdot \vec{d}$ = 12Jwork energy theorem  $W_{max} = \Delta K.E.$ 

$$12 = K_{f} - 3$$
  
 $K_{f} = 15J$ 

29. The Wheatstone bridge shown in Fig. here, gets balanced when the carbon resistor used as  $R_1$ has the colour code ( Orange, Red, Brown). The resistors  $R_2$  and  $R_4$  are 80 $\Omega$  and 40 $\Omega$ , respectively.

> Assuming that the colour code for the carbon resistors gives their accurate values, the colour code for the carbon resistor, used as R<sub>3</sub>, would be :



- (1) Red, Green, Brown
- (2) Brown, Blue, Brown
- (3) Grey, Black, Brown
- (4) Brown, Blue, Black

Ans. (2)  $R_1 = 32 \times 10 = 320$ for wheat stone bridge  $\Rightarrow \frac{R_1}{R_3} = \frac{R_2}{R_4}$  $\frac{320}{R_3} = \frac{80}{40}$  $R_3 = 160$ Blue Brown Brown

30. Two identical spherical balls of mass M and radius R each are stuck on two ends of a rod of length 2R and mass M (see figure). The moment of inertia of the system about the axis passing perpendicularly through the centre of the rod is :

$$(1) \frac{152}{15}MR^{2} \qquad (2) \frac{17}{15}MR^{2} \\ (3) \frac{137}{15}MR^{2} \qquad (4) \frac{209}{15}MR^{2}$$

Ans. (3)

For Ball using parallel axis theorem.

$$I_{ball} = \frac{2}{5}MR^2 + M(2R)^2$$
  
=  $\frac{22}{5}MR^2$ 

2 Balls so  $\frac{44}{5}$  MR<sup>2</sup>

Irod = for rod  $\frac{M(2R)^2}{R} = \frac{MR^2}{3}$  $I_{system} = I_{Ball} + I_{rod}$ 

$$= \frac{44}{5} MR^{2} + \frac{MR^{2}}{3}$$
$$= \frac{137}{15} MR^{2}$$

## TEST PAPER OF JEE(MAIN) EXAMINATION - 2019 (Held On Thrusday 10<sup>th</sup> JANUARY, 2019) TIME : 02 : 30 PM To 05 : 30 PM CHEMISTRY

1. An ideal gas undergoes isothermal compression from 5 m<sup>3</sup> against a constant external pressure of 4 Nm<sup>-2</sup>. Heat released in this process is used to increase the temperature of 1 mole of Al. If molar heat capacity of Al is 24 J mol<sup>-1</sup> K<sup>-1</sup>, the temperature of Al increases by :

(1) 
$$\frac{3}{2}$$
K (2)  $\frac{2}{3}$ K (3) 1 K (4) 2 K

Ans. (2)

**Sol.** Work done on isothermal irreversible for ideal gas

 $= -P_{ext} (V_2 - V_1)$ = -4 N/m<sup>2</sup> (1m<sup>3</sup> - 5m<sup>3</sup>) = 16 Nm Isothermal process for ideal gas  $\Delta U = 0$ q = -w = -16 Nm = - 16 J Heat used to increase temperature of A4

 $q = n C_m \Delta T$ 

$$16 J = 1 \times 24 \frac{J}{\text{mol.K}} \times \Delta T$$

$$\Delta T = \frac{2}{3}K$$

The 71<sup>st</sup> electron of an element X with an atomic number of 71 enters into the orbital : (1) 4f
(2) 6p
(3) 6s
(4) 5d

Ans. (1)

- The number of 2-centre-2-electron and 3-centre-2-electron bonds in B<sub>2</sub>H<sub>6</sub>, respectively, are :
  - (1) 2 and 4 (2) 2 and 1
  - (3) 2 and 2 (4) 4 and 2

### Ans. (4)

4. The amount of sugar (C<sub>12</sub>H<sub>22</sub>O<sub>11</sub>) required to prepare 2 L of its 0.1 M aqueous solution is : (1) 68.4 g (2) 17.1 g (3) 34.2 g (4)136.8 g
Ans. (1)

Ans. (1)

**Sol.** Molarity =  $\frac{(n)_{\text{solute}}}{V_{\text{solution}} (\text{in lit})}$ 

$$0.1 = \frac{\text{wt./342}}{2}$$
  
wt (C<sub>12</sub>H<sub>22</sub>O<sub>11</sub>) = 68.4 gram

5. Among the following reactions of hydrogen with halogens, the one that requires a catalyst is :

(1)  $H_2 + I_2 \rightarrow 2HI$  (2)  $H_2 + F_2 \rightarrow 2HF$ 

(3)  $H_2 + Cl_2 \rightarrow 2HCI$  (4)  $H_2 + Br_2 \rightarrow 2HBr$ 

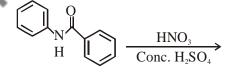
Ans. (1)

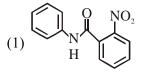
- 6. Sodium metal on dissolution in liquid ammonia gives a deep blue solution due to the formation of:
  - (1) sodium ion-ammonia complex
  - (2) sodamide
  - (3) sodium-ammonia complex
  - (4) ammoniated electrons

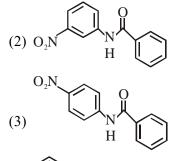
Ans. (4)

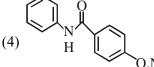
7.

What will be the major product in the following mononitration reaction?





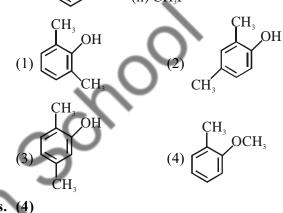




Ans. (3)

Sol. amine is o-p directing

- 8. In the cell  $Pt(s)|H_2(g, 1bar|HCl(aq)|Ag(s)|Pt(s)$ the cell potential is 0.92 when a 10<sup>-6</sup> molal HCl solution is used. THe standard electrode potential of (AgCl/Ag,Cl-) electrode is :  $\left\{ \text{given}, \frac{2.303\text{RT}}{\text{F}} = 0.06\text{Vat}298\text{K} \right\}$ 11. (1) 0.20 V (2) 0.76 V (3) 0.40 V (4) 0.94 V Ans. (1)  $Pt(s)|H_2(g, 1bar)|HCl(aq)|AgCl(s)|Ag(s)|Pt(s)$ Sol.  $10^{-6}$  m Anode:  $H_2 \longrightarrow 2H^+ + 2e \times 1$ Cathode :  $e^- + AgCl(s) \longrightarrow Ag(s) + Cl^-(aq)$ × 2  $H_2(g)l + AgCl(s) \longrightarrow 2H^+ +$  $2Ag(s) + 2Cl^{-}(aq)$  $E_{cell} = E_{cell}^{0} - \frac{0.06}{2} \log_{10} \left( (H^{+})^{2} \cdot (Cl^{-})^{2} \right)$  $.925 = \left(E^{0}_{H_{2}/H^{+}} + E^{0}_{AgCl/Ag, Cl^{-}}\right) - \frac{0.06}{2}\log_{10}$ Ans.  $((10^{-6})^2 (10^{-6})^2)$  $.92 = 0 + E^{0}_{AgCl/Ag,Cl^{-}} - 0.03 \log_{10}(10^{-6})^{4}$ 12.  $E_{AgCl}^0 / Ag, Cl^- = .92 + .03 \times -24 = 0.2 V$ The major product of the following recation is: 9. CH<sub>3</sub>N NaBH<sub>4</sub> ЭH (1)  $CH_{3}N$ QН 13. (2)  $CH_{3}N$ OH  $(3) CH_3N$ OH  $(4) CH_3N$ Ans. (3) An
- 10. The pair that contains two P-H bonds in each of the oxoacids is : (1)  $H_3PO_2$  nad  $H_4P_2O_5$ (2)  $H_4P_2O_5$  and  $H_4P_2O_6$ (3)  $H_3PO_3$  and  $H_3PO_2$ (4)  $H_4P_2O_5$  nad  $H_3PO_3$ Ans. (1) The major product of the following reaction is: OН (i) aq. NaOH



 $S_N^2$  reaction

The difference in the number of unpaired electrons of a metal ion in its high-spin and low-spin octahedral complexes is two. The metal ion is :

(1)  $Fe^{2+}$ (2)  $Co^{2+}$ (3)  $Mn^{2+}$ (4)  $Ni^{2+}$ 

Ans. (2)

**Sol.**  $Co^{2+} -->d^7$ hs, n = 3, ls, n = 1

A compound of formula  $A_2B_3$  has the hcp lattice. Which atom forms the hcp lattice and what fraction of tetrahedral voids is occupied by the other atoms :

	(1) hcp lattice-A, $\frac{2}{3}$ Tetrachedral voids-B
	(2) hcp lattice-B, $\frac{1}{3}$ Tetrachedral voids-A
	(3) hcp lattice-B, $\frac{2}{3}$ Tetrachedral voids-A
	(4) hcp lattice-A $\frac{1}{3}$ Tetrachedral voids-B
s.	(2)

**Sol.**  $A_2B_3$  has HCP lattice

If A form HCP, then  $\frac{3}{4}^{th}$  of THV must occupied by B to form  $A_2B_3$ 

If B form HCP, then  $\frac{1}{3}^{\text{th}}$  of THV must occupied by A to form  $A_2B_3$ 

- 14. The reaction that is NOT involved in the ozone layer depletion mechanism in the stratosphere is:
  - (1) HOCl(g)  $\xrightarrow{h\upsilon} OH(g) + Cl(g)$
  - (2)  $CF_2Cl_2(g) \xrightarrow{uv} Cl(g) + CF_2Cl(g)$
  - (3)  $CH_4 + 2O_3 \rightarrow 3CH_2 = O + 3H_2OP$
  - (4)  $\operatorname{ClO}(g) + \operatorname{O}(g) \rightarrow \operatorname{Cl}(g) + \operatorname{O}_2(g)$

Ans. (3)

Sol. Conceptual

15. The process with negative entropy change is :

- (1) Dissolution of iodine in water
- (2) Synthesis of ammonia from  $\mathrm{N}_2$  and  $\mathrm{H}_2$

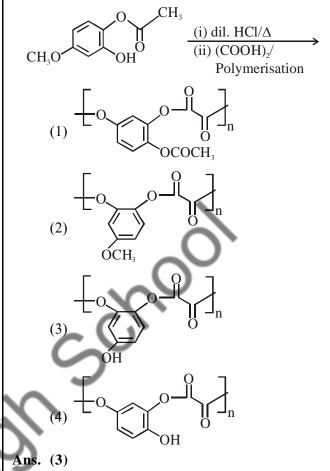
(3) Dissolution of  $CaSO_4(s)$  to CaO(s) and  $SO_3(g)$ 

(4) Subimation of dry ice

Ans. (2)

**Sol.**  $N_2(g) + 3H_2(g) \rightleftharpoons 2NH_3(g)$ ;  $\Delta n_{\sigma} < 0$ 

16. The major product of the following reaction is:

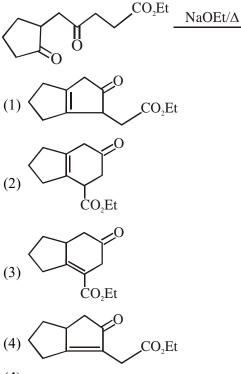


- 17. A reaction of cobalt(III) chloride and ethylenediamine in a 1 : 2 mole ratio generates two isomeric products A (violet coloured) B (green coloured). A can show optical activity, B is optically inactive. What type of isomers does A and B represent ?
  - (1) Geometrical isomers
  - (2) Ionisation isomers]
  - (3) Coordination isomers
  - (4) Linkage isomers

Ans. (1)

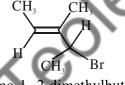
**Sol.** [Co(Cn)<sub>2</sub> Cl<sub>2</sub>]Cl cis --> Optically active trans --> Optically in active **18.** The major product obtained in the following reaction is :

22.



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Ans. (4)
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- **19.** Which of the following tests cannot be used for identifying amino acids ?
  - (1) Biuret test (2) Xanthoproteic test
  - (3) Barfoed test (4) Ninhydrin test
- Ans. (3)
- **20.** What is the IUPAC name of the following compound ?



- (1) 3-Bromo-1, 2-dimethylbut-1-ene]
- (2) 4-Bromo-3-methylpent-2-ene
- (3) 2-Bromo-3-methylpent-3-ene
- (4) 3-Bromo-3-methyl-1, 2-dimethylprop-1-ene
- Ans. (2)
- **21.** Which is the most suitable reagent for the following transformation ?

$$\begin{array}{c} & & & & & \\ & H \\ & CH_3-CH=CH-CH_2-CH-CH_3 \longrightarrow \\ & & CH_3-CH=CH-CH_2CO_2H \\ (1) \text{ alkaline KMnO}_4 \quad (2) \text{ I}_2/\text{NaOH} \\ (3) \text{ Tollen's reagent} \quad (4) \text{ CrO}_2/\text{CS}_2 \\ \textbf{Ans. (2)} \end{array}$$

Item 'I' Item 'II' (compound) (reagent) (A) Lysine (P) 1-naphthol (B) Furfural (Q) ninhydrin (C) Benzyl alcohol (R)  $KMnO_4$ (D) Styrene (S) Ceric ammonium nitrate (1) (A) $\rightarrow$ (Q), (B) $\rightarrow$ (P), (C) $\rightarrow$ (S), (D) $\rightarrow$ (R) (2) (A) $\rightarrow$ (Q), (B) $\rightarrow$ (R), (C) $\rightarrow$ (S), (D) $\rightarrow$ (P) (3) (A) $\rightarrow$ (Q), (B) $\rightarrow$ (P), (C) $\rightarrow$ (R), (D) $\rightarrow$ (S) (4) (A) $\rightarrow$ (R), (B) $\rightarrow$ (P), (C) $\rightarrow$ (Q), (D) $\rightarrow$ (S) Ans. (1) In the reaction of oxalate with permaganate in acidic 23. medium, the number of electrons involved in producing one molecule of CO<sub>2</sub> is : (4) 5(1) 10(2) 2(3) 1 Ans. (3)  $5C_2O_4^{2-} + 16H^+ \longrightarrow 2Mn^{2+}$  $MnO_4$ Sol.  $+10CO_{2} + 8H_{2}O_{2}$ 10 e<sup>-</sup> trans for 10 molecules of CO<sub>2</sub> so per molecule of CO<sub>2</sub> transfer of e<sup>-</sup> is '1' 24. 5.1g  $NH_4SH$  is introduced in 3.0 L evacuated flask at 327°C. 30% of the solid NH<sub>4</sub>SH decomposed to NH<sub>3</sub> and H<sub>2</sub>S as gases. The K<sub>p</sub> of the reaction at  $327^{\circ}$ C is (R = 0.082 L atm  $mol^{-1}K^{-1}$ , Molar mass of S = 32 g mol<sup>/01</sup>, molar mass of N = 14g mol<sup>-1</sup>) (1)  $1 \times 10^{-4} \text{ atm}^2$ (2)  $4.9 \times 10^{-3}$  atm<sup>2</sup> (3)  $0.242 \text{ atm}^2$ (4)  $0.242 \times 10^{-4} \text{ atm}^2$ Ans. (3)  $NH_4SH(s) \Longrightarrow NH_3(g) + H_2S(g)$ **Sol.**  $n = \frac{5.1}{51} = .1 \text{ mole} = 0$ 0  $.1(-1-\alpha)$ .1α .1α  $\alpha = 30\% = .3$ so number of moles at equilibrium  $.1 (1 - .3) .1 \times .3$  $.1 \times .3$ .07 =.03=.03Now use PV = nRT at equilibrium  $P_{total} \times 3 \text{ lit} = (.03 + .03) \times .082 \times 600$  $P_{total} = .984 atm$ At equilibrium  $P_{\rm NH_3} = P_{\rm H_2S} = \frac{P_{\rm total}}{2} = .492$ So  $k_p = P_{NH_3} \cdot P_{H_2S} = (.492) (.492)$  $k_p = .242 \text{ atm}^2$ 

The correct match between item 'I' and item 'II' is :

**25.** The electrolytes usually used in the electroplating of gold and silver, respectively, are :

- (1)  $[Au(OH)_4]^-$  and  $[Ag(OH)_2]^-$
- (2)  $[Au(CN)_2]^-$  and  $[Ag CI_2]^-$
- (3)  $[Au(NH_3)_2]^+$  and  $[Ag(CN)_2]^-$
- (4)  $[Au(CN)_2]^-$  and  $[Ag(CN)_2]^-$

### Ans. (4)

26. Elevation in the boiling point for 1 molal solution of glucose is 2 K. The depression in the freezing point of 2 molal solutions of glucose in the same solvent is 2 K. The relation between  $K_b$  and  $K_f$  is:

(1) 
$$K_b = 0.5 K_f$$
 (2)  $K_b = 2 K_f$   
(3)  $K_b = 1.5 K_f$  (4)  $K_b = K_f$ 

Ans. (2)

Sol. Ans.(2)

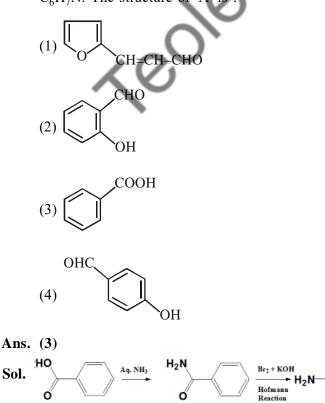
 $\frac{\Delta T_{b}}{\Delta T_{f}} = \frac{i.m \times k_{b}}{i \times m \times k_{f}}$   $2 \quad 1 \times 1 \times k_{b}$ 

$$\frac{1}{2} = \frac{1}{1 \times 2 \times k}$$

 $k_b = 2k_f$ 

Benzoic acid

27. An aromatic compound 'A' having molecular formula  $C_7H_6O_2$  on treating with aqueous ammonia and heating forms compound 'B'. The compound 'B' on reaction with molecular bromine and potassium hydroxide provides compound 'C' having molecular formula  $C_6H_7N$ . The structure of 'A' is :



Benzamide

28. The ground state energy of hydrogen atom is -13.6 eV. The energy of second excited state He<sup>+</sup> ion in eV is : (1) -6.04 (2) -27.2 (3) -54.4 (4) -3.4

**Ans.** (1)

**Sol.** 
$$(E)_{n^{th}} = (E_{GND})_H \cdot \frac{Z^2}{n^2}$$

$$E_{3^{rd}}(He^+) = (-13.6 \text{ eV}) \cdot \frac{2^2}{3^2} = -6.04 \text{ eV}$$

29. For an elementary chemical reaction,

$$A_{2} \xleftarrow{k_{1}}{k_{-1}} 2A, \text{ the expression for } \frac{d[A]}{dt} \text{ is }:$$
(1)  $2k_{1}[A_{2}]-k_{-1}[A]^{2}$  (2)  $k_{1}[A_{2}]-k_{-1}[A]^{2}$ 
(3)  $2k_{1}[A_{2}]-2k_{-1}[A]^{2}$  (4)  $k_{1}[A_{2}]+k_{-1}[A]^{2}$ 
Ans. (3)
Sol. Ans.(3)
 $A_{2} \xleftarrow{k_{1}}{K_{-1}} 2A$ 
 $\frac{d[A]}{dt} = 2k_{1}[A_{2}]-2k_{-1}[A]^{2}$ 

- 30. Haemoglobin and gold sol are examples of :(1) negatively charged sols
  - (2) positively charged sols]
  - (3) negatively and positively charged sols, respectively
  - (4) positively and negatively charged sols, respectively

Ans. (4)

Aniline

(C<sub>6</sub>H<sub>7</sub>N)

### Sol. Ans.(4)

Haemoglobin  $\longrightarrow$  positive sol Ag - sol  $\longrightarrow$  negative sol

# **TEST PAPER OF JEE(MAIN) EXAMINATION – 2019** (Held On Thursday 10<sup>th</sup> JANUARY, 2019) TIME : 2 : 30 PM To 5 : 30 PM MATHEMATICS

1. Let 
$$z = \left(\frac{\sqrt{3}}{2} + \frac{1}{2}\right)^{3} + \left(\frac{\sqrt{3}}{2} - \frac{1}{2}\right)^{3}$$
. If  $R(z)$  and  $I[z]$   
respectively denote the real and imaginary parts  
of  $z$ , then :  
(1)  $R(z) > 0$  and  $I(z) > 0$   
(2)  $R(z) < 0$  and  $I(z) > 0$   
(3)  $R(z) = -3$   
(4)  $I(z) = 0$   
Ans. (4)  
Sol.  $z = \left(\frac{\sqrt{3} + i}{2}\right)^{3} + \left(\frac{\sqrt{3} - i}{2}\right)^{3}$   
 $z = \left(e^{1zr(x)}\right)^{3} + \left(e^{-1zr(x)}\right)^{3}$   
 $z = \left(e^{1zr(x)}\right)^{3} + \left(e^{1zr(x)}\right)^{3}$   
 $z = \left(e^{1zr(x)}\right)^{3} + \left(e^{1zr(x)}\right)^{3}$   
 $z = \left(e^{1zr(x)}\right)^{3} + \left(e^{1zr(x)}\right)^{3}$   
 $z = \left(e^{1zr(x)}\right)^{3} + \left(e^{1zr(x)}\right)^$ 

5. The value of 
$$\int_{x_2}^{x_2} \frac{dx}{|x| + |\sin x| + 4}$$
 where [1]  
denotes the greatest integer less than or equal  
to t, is :  
(1)  $\frac{1}{12}(7\pi + 5)$  (2)  $\frac{3}{10}(4\pi - 3)$   
(3)  $\frac{1}{12}(7\pi - 5)$  (4)  $\frac{3}{20}(4\pi - 3)$   
(3)  $\frac{1}{12}(7\pi - 5)$  (4)  $\frac{3}{20}(4\pi - 3)$   
Ans. (4)  
Sol.  $1 = \int_{\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{dx}{(x| + |\sin x| + 4)}$   
Sol.  $1 = \int_{\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{dx}{(x| + |\sin x| + 4)}$   
 $= \int_{\frac{\pi}{2}}^{\frac{1}{2}} \frac{dx}{(x| - 1 - 1 + 4)} + \int_{\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{dx}{(1 - 1 - 1 + 4)}$   
 $= \int_{\frac{\pi}{2}}^{\frac{1}{2}} \frac{dx}{(1 - 1 - 1 + 4)} + \int_{\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{dx}{(1 - 1 - 1 + 4)}$   
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 $= \int_{\frac{\pi}{2}}^{\frac{1}{2}} \frac{dx}{(1 + 0 + 4)} + \int_{\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{dx}{(1 - 1 - 1 + 4)}$   
 $= \int_{\frac{\pi}{2}}^{\frac{1}{2}} \frac{dx}{(1 + 1 - \frac{\pi}{4})} + \int_{\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{dx}{(1 - 1 - 1 + 4)}$   
 $= \int_{\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{dx}{(1 + 1 - \frac{\pi}{4})} + \int_{\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{dx}{(1 - 1 - 1 + 4)}$   
 $= \int_{\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{dx}{(1 - 1 - 1 + 4)} + \int_{\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{dx}{(1 - 1 - 1 + 4)}$   
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 $= \int_{\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{dx}{(1 - 0 + 4)} + \int_{\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{dx}{(1 - 1 - 1 + 4)}$   
 $= \int_{\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{dx}{(1 - 1 - 1 + 4)} + \int_{\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{dx}{(1 - 1 - 1 + 4)} + \int_{\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{dx}{(1 - 1 - 1 + 4)}$   
 $= \int_{\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{dx}{(1 - 1 - 1 + 4)} + \int_{\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{dx}{(1 - 1 - 1 + 4)} + \int_{\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{dx}{(1 - 1 - 1 + 4)} + \int_{\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{dx}{(1 - 1 - 1 + 4)} + \int_{\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{dx}{(1 - 1 - 1 + 4)} + \int_{\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{dx}{(1 - 1 - 1 + 4)} + \int_{\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{dx$ 

If the probability of hitting a target by a shooter,

Sol. 
$$x^{2} = 4y$$
  
 $x - \sqrt{2}y + 4\sqrt{2} = 0$   
Solving together we get  
 $x^{3} = 4\left(\frac{x+4\sqrt{2}}{\sqrt{2}}\right)$   
 $\sqrt{2}x^{2} + 4x + 16\sqrt{2}$   
 $\sqrt{2}x^{2} - 4x - 16\sqrt{2} = 0$   
 $x_{1} + x_{2} = 2\sqrt{2}; \quad x_{1}x_{2} = \frac{-16\sqrt{2}}{\sqrt{2}} = -16$   
Similarly,  
 $\left(\sqrt{2}y - 4\sqrt{2}\right)^{2} - 4y$   
 $2y^{2} + 32 - 16y = 4y$   
 $2y^{2} - 20y + 32 = 0$   
 $y', \pm y', = 10$   
 $y', \pm y', = 10$   
 $y', 2y' - 20y + 32 = 0$   
 $y', \pm y', = 16$   
 $\frac{\sqrt{2}}{(x_{0}, y_{1})}$   
 $\ell_{AB} = \sqrt{(x_{0} - x_{1})^{2} + (y_{0} - y_{1})^{2}}$   
 $= \sqrt{(2\sqrt{2})^{2} + 64 + (100^{2} - 4106)}$   
 $= \sqrt{8 + 64 + 100 - 64}$   
 $= \sqrt{1068} - 6\sqrt{3}$   
Option (3)  
9. Let  $A = \begin{bmatrix} 2 & b & 1 \\ \sqrt{3} & (2) & -\sqrt{3}$   
 $(1) \sqrt{3} & (2) & -\sqrt{3}$   
 $(1) \sqrt{3} & (2) & -\sqrt{3}$   
 $(1) \sqrt{3} & (2) & -\sqrt{3}$   
 $(3) - 2\sqrt{3} & (4) 2\sqrt{3}$   
Ans. (4)  
Sol.  $A = \begin{bmatrix} 2 & b & 1 \\ b & b^{2} + 1 & b \\ 1 & b & 2 \end{bmatrix}$  (b)  $A = 2(2b^{2} + 2 - b^{2} - b(2b - b) + 1 (b^{2} - b^{2} - 1)$   
 $|A| = 2(2b^{2} + 2 - b^{2} - 1)(2b - b) + 1 (b^{2} - b^{2} - 1)$   
 $|A| = 2(2b^{2} + 2 - b^{2} - b(2b - b) + 1 (b^{2} - b^{2} - 1)$   
 $|A| = b^{3} + 3$   
 $A = \frac{b^{3}}{b} \Rightarrow \sqrt{3}$   
 $b + \frac{3}{b} \ge 2\sqrt{3}$   
 $b + \frac{3}{b} \ge 2\sqrt{3$ 

Sol. 
$$\begin{vmatrix} 1 & 3 & 7 \\ -1 & 4 & 7 \\ sin 30 & cos 20 & 2 \end{vmatrix}$$
  
(8 - 7 cos 20 - 3(-2 - 7 sin 30)  
+ 7 (- cos 20 - 4 sin 30) = 0  
14 - 7 (sin 30 - 14 cos 20 = 0  
-2 2 sin 30 - 7 cos 20  
-2 2 sin 30 - 14 (1 - 2 sin<sup>2</sup> 0) = 0  
-21 sin 0 + 28 sin<sup>2</sup> 0 + 28 sin<sup>2</sup> 0 = 0  
-21 sin 0 + 28 sin<sup>2</sup> 0 + 28 sin<sup>2</sup> 0 = 0  
-21 sin 0 + 28 sin<sup>2</sup> 0 + 28 sin<sup>2</sup> 0 = 0  
7 sin 0 (-3 + 4 sin<sup>2</sup> 0) + 4 sin 0 ] = 0  
sin 0 =  $\frac{-3}{2}$ ; sin 0 =  $\frac{1}{2}$   
Hence, 2 solutions in (0,  $\pi$ )  
Option (4)  
12. If  $\int_{0}^{1} f(t) dt = x^{2} + \int_{0}^{1} t^{2} f(t) dt$ , then  $f(1/2)$  is :  
(1)  $\frac{6}{25}$  (2)  $\frac{24}{25}$   
(3)  $\frac{18}{25}$  (4)  $\frac{4}{5}$   
Ans. (2)  
Sol.  $\int_{0}^{1} f(t) dt = x^{2} + \int_{0}^{1} t^{2} f(t) dt$   
f(x) =  $\frac{2x}{1 + x^{2}}$   $\Rightarrow$  f(x) =  $\frac{(1 + x^{2})^{2} - 2x(2x)}{(1 + x)^{7}}$   
f(x) =  $\frac{2x^{2} - 4x^{2} + 2}{(1 + x)^{2}}$   
f(x) =  $\frac{2x^{2} - 4x^{2} + 2}{(1 + x)^{2}}$   
f(x) =  $\frac{2x^{2} - 4x^{2} + 2}{(1 + x)^{2}}$   
f(x) =  $\frac{2x^{2} - 4x^{2} + 2}{(1 + x)^{2}}$   
 $f(x) = (2)$   
A subset of the second second

Ans. (4)  
Sol. 
$$\frac{y^2}{1+r} - \frac{x^2}{1-r} = 1$$
for  $r > 1$ , 
$$\frac{y^2}{1+r} + \frac{x^2}{r-1} = 1$$
 $c = \sqrt{1 - \left(\frac{r-1}{r+1}\right)}$ 
 $= \sqrt{\frac{1-(r-1)}{(r+1)}}$ 
 $= \sqrt{\frac{1-(r-1)}{(r+1)}}$ 
 $= \sqrt{\frac{2}{r+1}} = \sqrt{\frac{2}{r+1}}$ 
Option (4)  
15. If  $\sum_{i=0}^{3} [e^3C, e^{-9\sigma}C_{3x-i}] = K(e^3C_{3x})$ , then K is equal to :  
(1)  $2^{25} - 1$  (2)  $(25)^2$  (3)  $2^{25}$  (4)  $2^{24}$   
Ans. (3)  
Sol.  $\sum_{i=0}^{3} e^3C_i, e^{-9\sigma}C_{3x-i}] = K(e^3C_{3x})$ , then K is equal to :  
(1)  $2^{25} - 1$  (2)  $(25)^2$  (3)  $2^{25}$  (4)  $2^{24}$   
Ans. (3)  
Sol.  $\sum_{i=0}^{3} e^3C_i, e^{-9\sigma}C_{3x-i}] = K(e^{2s}C_{3x})$ , then K is equal to :  
(1)  $2^{25} - 1$  (2)  $(25)^2$  (3)  $2^{25}$  (4)  $2^{24}$   
Ans. (3)  
Sol.  $\sum_{i=0}^{3} e^3C_i, e^{-9\sigma}C_{3x-i}$   
 $= \sum_{i=0}^{3} \frac{50!}{r(50-r)!} \times \frac{(50-r)!}{(25)^2(25-r)!}$   
 $= \sum_{i=0}^{3} \frac{50!}{r(50-r)!} \times \frac{(50-r)!}{(25)^2(25-r)!}$   
 $= \sum_{i=0}^{3} \frac{50!}{r(25-r)!} \times \frac{(50-r)!}{(25)^2(25-r)!}$   
 $= \sum_{i=0}^{3} \frac{15}{(25-r)!} (a + \beta)^2 - 2\alpha\beta = (\lambda - 3)^2 - 2(2 - \lambda)$   
 $= \lambda^2 + 9 - 6\lambda - 4 + 2\lambda$   
 $= \lambda^2 - 4\lambda + 5$   
 $= (\lambda - 2)^2 + 1$   
 $\therefore \lambda = 2$   
Option (1)  
18. Two vertices of a triangle are (0.2) and (4.3).  
If its orthocenere is at the origin, then its third vertex lies in which quadrant ?  
(1) Fourth  
(2) Second  
(3) Third  
(4) First  
Ans. (4)

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Let  $\vec{\alpha} = (\lambda - 2)\vec{a} + \vec{b}$  and  $\vec{\beta} = (4\lambda - 2)\vec{a} + 3\vec{b}$ 20. be **Sol.**  $m_{BD} \times m_{AD} = -1 \implies \left(\frac{3-2}{4-0}\right) \times \left(\frac{b-0}{a-0}\right) = -1$ two given vectors where vectors  $\vec{a}$  and  $\vec{b}$  are  $\Rightarrow$  b + 4a = 0 .....(i) non-collinear. The value of  $\lambda$  for which vectors A(a, b) $\vec{\alpha}$  and  $\vec{\beta}$  are collinear, is : (1) - 3(2) 4 (3) 3 (4) - 4Ans. (4) B **Sol.**  $\vec{\alpha} = (\lambda - 2)\vec{\alpha} + \vec{b}$ (0, 2) (4, 3) $\vec{\beta} = (4\lambda - 2)\vec{\alpha} + 3\vec{b}$  $m_{AB} \times m_{CF} = -1 \implies \left(\frac{(b-2)}{a-0}\right) \times \left(\frac{3}{4}\right) = -1$  $\frac{\lambda-2}{4\lambda-2} = \frac{1}{3}$  $\Rightarrow$  3b - 6 = -4a  $\Rightarrow$  4a + 3b = 6 .....(ii)  $3\lambda - 6 = 4\lambda - 2$  $\frac{\lambda = -4}{\cdot \text{ Option (4)}}$ From (i) and (ii)  $a = \frac{-3}{4}, b = 3$ The value of  $\cot\left(\sum_{n=1}^{19} \cot^{-1}\left(1 + \sum_{p=1}^{n} 2p\right)\right)$  is : ∴ II<sup>nd</sup> quadrant. 21. Option (2) 19. Two sides of a parallelogram are along the  $\frac{22}{23} \qquad (2) \ \frac{23}{22} \qquad (3) \ \frac{21}{19} \qquad (4) \ \frac{19}{21}$ lines, x + y = 3 and x - y + 3 = 0. If its diagonals intersect at (2,4), then one of its vertex is : **Ans.** (3) (1) (2,6)(2)(2,1)**Sol.**  $\cot\left(\sum_{n=1}^{19}\cot^{-1}(1+n(n+1))\right)$ (4) (3,6)(3) (3,5)Ans. (4)  $\cot\left(\sum_{n=1}^{19}\cot^{-1}(n^2+n+1)\right) = \cot\left(\sum_{n=1}^{19}\tan^{-1}\frac{1}{1+n(n+1)}\right)$  $\sum_{i=1}^{19} (\tan^{-1}(n+1) - \tan^{-1}n)$ **Sol.** x + y = -3 $B(x_{2}, x_{2})$  $\cot (\tan^{-1}20 - \tan^{-1}1) = \frac{\cot A \cot \beta + 1}{\cot \beta - \cot A}$ x + y = 3  $\sum_{x - y = -3}^{A(0, 3)}$ Solving  $\frac{1\left(\frac{1}{20}\right)+1}{1-\frac{1}{20}} = \frac{21}{19}$ and (Where tanA=20, tanB=1)  $\frac{x_1+0}{2} = 2; x_i = 4$  similarly  $y_1 = 5$  $\therefore$  Option (3)  $C \Rightarrow (4, 5)$ 22. With the usual notation, in  $\triangle ABC$ , if Now equation of BC is x - y = -1 $\angle A + \angle B = 120^{\circ}, a = \sqrt{3} + 1 \text{ and } b = \sqrt{3} - 1,$ and equation of CD is x + y = 9Solving x + y = 9 and x - y = -3then the ratio  $\angle A : \angle B$ , is : Point D is (3, 6)(1) 7 : 1(2) 5 : 3Option (4) (3) 9 : 7(4) 3 : 1

Ans. (1)  
Sol. 
$$A + B = 120^{\circ}$$
  
 $a + B = 120^{\circ}$   
 $a + B = \frac{1}{2} - \frac{1}{2} - \frac{1}{2} - \frac{1}{2} - \frac{1}{2}$   
 $a = \frac{\sqrt{3} + 1 - \sqrt{3} + 1}{2(\sqrt{3})} - col(30^{\circ}) = \frac{1}{\sqrt{3}} - \sqrt{3} = 1$   
 $a = \frac{\sqrt{3} + 1 - \sqrt{3} + 1}{2(\sqrt{3})} - col(30^{\circ}) = \frac{1}{\sqrt{3}} - \sqrt{3} = 1$   
 $a = \frac{\sqrt{3} + 1 - \sqrt{3} + 1}{2(\sqrt{3})} - col(30^{\circ}) = \frac{1}{\sqrt{3}} - \sqrt{3} = 1$   
 $a = \frac{\sqrt{3} + 1 - \sqrt{3} + 1}{2(\sqrt{3})} - col(30^{\circ}) = \frac{1}{\sqrt{3}} - \sqrt{3} = 1$   
 $a = \frac{\sqrt{3} + 1 - \sqrt{3} + 1}{2(\sqrt{3})} - col(30^{\circ}) = \frac{1}{\sqrt{3}} - \sqrt{3} = 1$   
 $a = \frac{\sqrt{3} + 1 - \sqrt{3} + 1}{2(\sqrt{3})} - col(30^{\circ}) = \frac{1}{\sqrt{3}} - \sqrt{3} = 1$   
 $a = \frac{\sqrt{3} + 1 - \sqrt{3} + 1}{2(\sqrt{3})} - col(30^{\circ}) = \frac{1}{\sqrt{3}} - \sqrt{3} = 1$   
 $a = \frac{\sqrt{3} + 1 - \sqrt{3} + 1}{2(\sqrt{3})} - col(30^{\circ}) = \frac{1}{\sqrt{3}} - \sqrt{3} = 1$   
 $a = \frac{\sqrt{3} + 1 - \sqrt{3} + 1}{2(\sqrt{3})} - col(30^{\circ}) = \frac{1}{\sqrt{3}} - \sqrt{3} = 1$   
 $a = \frac{\sqrt{3} - 2}{2(\sqrt{3})} - \frac{2}{2(\sqrt{3})} - \frac{2}{2(\sqrt{3})}$ 

26. Let f be a differentiable function such that  

$$f'(x) = 7 - \frac{3}{4} \frac{f(x)}{x}, (x > 0) \text{ and } f(1) \neq 4.$$
Then  $\lim_{x \to 0^+} f(\frac{1}{x})$ :  
(1) Exists and equals 4  
(2) Does not exist  
(3) Exist and equals 0  
(4) Exists and equals 0  
(4) Exists and equals 0  
(4) Exists and equals  $\frac{4}{7}$   
Ans. (1)  
Sol.  $f'(x) = 7 - \frac{3}{4} \frac{f(x)}{x}, (x > 0)$   
Given  $f(1) \neq 4$   $\lim_{x \to 0^+} xf(\frac{1}{x}) = ?$   
 $\frac{dy}{dx} + \frac{3}{4x} = 7$  (This is LDE)  
IF  $= e^{\int_{x}^{\frac{2}{4}} e^{-\frac{2}{3}\frac{1}{4}x}}, (x > 0)$   
 $g(x) = \frac{1}{7}, x^{\frac{3}{4}} dx$   
 $y, x^{\frac{3}{4}} = \frac{2}{7}, x^{\frac{3}{4}} dx$   
 $f(x) = 4x + Cx^{-\frac{3}{4}}$   
 $f(\frac{1}{x}) = \frac{4}{x} + Cx^{\frac{2}{4}}$   
 $\lim_{x \to 0} xf(\frac{1}{x}) = \frac{1}{x}$   
 $\frac{1}{x} = \frac{1}{x}$   
 $\frac{1}{x} = \frac{1}{x}$   
 $\frac{1}{x} = \frac{1}{x} = \frac{1}{x}$   
 $\frac{1}{x} = \frac{1}{x} = \frac{1}{x} = \frac{1}{x}$   
 $y, x^{\frac{3}{4}} = 7, (\frac{1}{x})$   
 $\frac{1}{x} = \frac{1}{x} = \frac{1}{x} = \frac{1}{x}$   
 $\frac{1}{x} = \frac{1}{x} = \frac{1}$ 

29. The curve amongst the family of curves, If  $\int x^5 e^{-4x^3} dx = \frac{1}{48} e^{-4x^3} f(x) + C$ , where C is a 28. represented by the differential equation,  $(x^2 - y^2)dx + 2xy dy = 0$  which passes through constant of integration, then f(x) is equal to : (1,1) is :  $(1) - 4x^3 - 1$ (2)  $4x^3 + 1$ (1) A circle with centre on the y-axis  $(3) -2x^3 - 1 \qquad (4) -2x^3 + 1$ (2) A circle with centre on the x-axis Ans. (1) (3) An ellipse with major axis along the y-axis **Sol.**  $\int x^5 \cdot e^{-4x^3} dx = \frac{1}{48} e^{-4x^3} f(x) + c$ (4) A hyperbola with transverse axis along the x-axis Put  $x^3 = t$ Ans. (2)  $3x^2 dx = dt$ **Sol.**  $(x^2 - y^2) dx$  $\int x^3 \cdot e^{-4x^3} \cdot x^2 dx$  $\frac{1}{3}\int t \cdot e^{-4t} dt$ Put  $y = vx \implies \frac{dy}{dx} = v + x \frac{dv}{dx}$  $\frac{1}{3}\left[t \cdot \frac{e^{-4t}}{-4} - \int \frac{e^{-4t}}{-4} dt\right]$ Solving we get,  $\int \frac{2v}{v^2 + 1} dv = \int -\frac{dx}{x}$  $-\frac{e^{-4t}}{48}[4t+1]+c$  $\ln(v^2 + 1) = -\ln x + C$  $(y^2 + x^2) = Cx$  $1 + 1 = C \Rightarrow C = 2$  $\therefore$  f(x) = -1 - 4x<sup>3</sup>  $y^2 + x^2 = 2x$ Option (1)  $\therefore$  Option (2) (From the given options (1) is most suitable)

