TEST PAPER OF JEE(MAIN) EXAMINATION – 2019 (Held On Friday 11th JANUARY, 2019) TIME : 9 : 30 AM To 12 : 30 PM PHYSICS

1. A body is projected at t = 0 with a velocity 10 ms⁻¹ at an angle of 60° with the horizontal. The radius of curvature of its trajectory at t = 1s is R. Neglecting air resistance and taking acceleration due to gravity g = 10 ms⁻², the value of R is :

(1) 2.5 m	(2) 10.3 m
(3) 2.8 m	(4) 5.1 m

Ans. (3)

Ans.



$$v_{x} = 10\cos 60^{\circ} = 5 \text{ m/s}$$

$$v_{y} = 10\cos 30^{\circ} = 5\sqrt{3} \text{ m/s}$$
velocity after t = 1 sec.
$$v_{x} = 5 \text{ m/s}$$

$$v_{y} = \left| (5\sqrt{3}-10) \right| \text{m/s} = 10 - 5\sqrt{3}$$

$$a_{n} = \frac{v^{2}}{R} \Rightarrow R = \frac{v_{x}^{2} + v_{y}^{2}}{a_{n}} = \frac{25+100+75-100\sqrt{3}}{10\cos\theta}$$

$$\tan\theta = \frac{10-5\sqrt{3}}{5} = 2-\sqrt{3} \Rightarrow \theta = 15^{\circ}$$

$$R = \frac{100(2-\sqrt{3})}{10\cos 15} = 2.8\text{m}$$

2. A particle is moving along a circular path with a constant speed of 10 ms^{-1} . What is the magnitude of the change in velocity of the particle, when it moves through an angle of 60° around the centre of the circle?

(1) zero	(2) 10 m/s
(3) $10\sqrt{3}$ m/s	(4) $10\sqrt{2}$ m/s
(2)	



A liquid of density β is coming out of a hose pipe of radius a with horizontal speed v and hits a mesh. 50% of the liquid passes through the mesh unaffected. 25% looses all of its momentum and 25% comes back with the same speed. The resultant pressure on the mesh will be :

(1)
$$\rho v^2$$
 (2) $\frac{3}{4}\rho v^2$

(3)
$$\frac{1}{2}\rho v^2$$
 (4) $\frac{1}{4}\rho v^2$

Ans. (2)

1

Sol. Momentum per second carried by liquid per second is ρav^2

net force due to reflected liquid = $2 \times \left[\frac{1}{4}\rho a v^2\right]$

net force due to stopped liquid = $\frac{1}{4}\rho av^2$

- Total force = $\frac{3}{4}\rho av^2$ net pressure = $\frac{3}{4}\rho v^2$
- 5. An electromagnetic wave of intensity 50 Wm⁻² enters in a medium of refractive index 'n' without any loss. The ratio of the magnitudes of electric fields, and the ratio of the magnitudes of magnetic fields of the wave before and after entering into the medium are respectively, given by :

(1)
$$\left(\frac{1}{\sqrt{n}}, \frac{1}{\sqrt{n}}\right)$$

(2) $\left(\sqrt{n}, \frac{1}{\sqrt{n}}\right)$
(3) $\left(\sqrt{n}, \sqrt{n}\right)$
(4) $\left(\frac{1}{\sqrt{n}}, \sqrt{n}\right)$
Ans. (2)
Sol. $C = \frac{1}{\sqrt{\mu_0 \epsilon_0}}$ [For transparent medium $\mu_r \approx \mu_0$]
 $\therefore \frac{C}{V} = \sqrt{k} = n$
 $\frac{1}{2} \epsilon_0 E_0^2 C = \text{intensity} = \frac{1}{2} \epsilon_0 k E^2 v$
 $\therefore E_0^2 C = k E^2 v$

$$\Rightarrow \frac{E_0^2}{E^2} = \frac{kV}{C} = \frac{n^2}{n} \Rightarrow \frac{E_0}{E} = \sqrt{n}$$

similarly

$$\frac{B_0^2 C}{2\mu_0} = \frac{B^2 v}{2\mu_0} \Longrightarrow \frac{B_0}{B} = \frac{1}{\sqrt{n}}$$

6. An amplitude modulated signal is given by $V(t) = 10[1 + 0.3\cos(2.2 \times 10^4)]\sin(5.5 \times 10^5 t).$ Here t is in seconds. The sideband frequencies (in kHz) are, [Given $\pi = 22/7$] (1) 1785 and 1715 (2) 892.5 and 857.5 (3) 89.25 and 85.75 (4) 178.5 smf 171.5 Ans. (3) $V(t) = 10 + \frac{3}{2} \left[2\cos A \sin B \right]$ Sol. $=10+\frac{3}{2}[\sin(A+B)-\sin(A-B)]$ $=10+\frac{3}{2}[\sin(57.2\times10^4 t)-\sin(52.8\times10^4 t)]$ $\omega_1 = 57.2 \times 10^4 = 2\pi f_1$ $f_1 = \frac{57.2 \times 10^4}{2 \times \left(\frac{22}{7}\right)} = 9.1 \times 10^4$ $\simeq 91 \text{KHz}$ $f_2 = \frac{52.8 \times 10^4}{2 \times \left(\frac{22}{7}\right)}$ $\simeq 84 \, \text{KHz}$ Side band frequency are $f_1 = f_c - f_w = \frac{52.8 \times 10^4}{2\pi} \approx 85.00 \text{ kHz}$

$$f_2 = f_c + f_w = \frac{57.2 \times 10^4}{2\pi} \approx 90.00 \text{ kHz}$$

7. The force of interaction between two atoms is

given by
$$F = \alpha \beta \exp\left(-\frac{x^2}{\alpha kt}\right)$$
; where x is the

distance, k is the Boltzmann constant and T is temperature and α and β are two constants. The dimension of β is :

- (1) $M^2L^2T^{-2}$
- (2) $M^{2}LT^{-4}$
- (3) $M^0L^2T^{-4}$
- (4) MLT^{-2}

Ans. (2)

Sol. $F = \alpha \beta e^{\left(\frac{-x^2}{\alpha KT}\right)}$

$$\left[\frac{x^2}{\alpha KT}\right] = M^{\circ}L^{\circ}T^{\circ}$$

$$\frac{L^{2}}{[\alpha]ML^{2}T^{-2}} = M^{\circ}L^{\circ}T^{\circ}$$
$$\Rightarrow [\alpha] = M^{-1}T^{2}$$
$$[F] = [\alpha] [\beta]$$
$$MLT^{-2} = M^{-1}T^{2}[\beta]$$
$$\Rightarrow [\beta] = M^{2}LT^{-4}$$

8. The charges Q + q and +q are placed at the vertices of a right-angle isosceles triangle as shown below. The net electrostatic energy of the configuration is zero, it the value of Q is:



(1)
$$\frac{-\sqrt{2q}}{\sqrt{2}+1}$$
 (2) $-2q$

(3)
$$\frac{-q}{1+\sqrt{2}}$$
 (4) +q

Ans. (1)

Sol. U = K
$$\left[\frac{q^2}{a} + \frac{Qq}{a} + \frac{Qq}{a\sqrt{2}} \right] = 0$$

9. In the circuit shown,



the switch S_1 is closed at time t = 0 and the switch S_2 is kept open. At some later time (t_0) , the switch S_1 is opened and S_2 is closed. The behaviour of the current I as a function of time 't' is given by :







Ans. (2)

Sol. From time t = 0 to $t = t_0$, growth of current takes place and after that decay of current takes place.



most appropriate is (2)

10. Equation of travelling wave on a stretched string of linear density 5 g/m is $y = 0.03 \sin(450 t - 9x)$ where distance and time are measured is SI units. The tension in the string is :

Ans. (2)

Sol. $y = 0.03 \sin(450 t - 9x)$

$$v = \frac{\omega}{k} = \frac{450}{9} = 50 \text{ m/s}$$
$$v = \sqrt{\frac{T}{\mu}} \Rightarrow \frac{T}{\mu} = 2500$$
$$\Rightarrow T = 2500 \times 5 \times 10^{-3}$$
$$= 12.5 \text{ N}$$

11. An equilateral triangle ABC is cut from a thin solid sheet of wood. (see figure) D, E and F are the mid-points of its sides as shown and G is the centre of the triangle. The moment of inertia of the triangle about an axis passing through G and perpendicular to the plane of the triangle is I_0 . It the smaller triangle DEF is removed from ABC, the moment of inertia of the remaining figure about the same axis is I. Then:



Ans. (4)

Sol. Suppose M is mass and a is side of larger triangle, then
$$\frac{M}{4}$$
 and $\frac{a}{2}$ will be mass and side length of smaller triangle.

$$\frac{I_{removed}}{I_{original}} = \frac{\frac{M}{4}}{M} \cdot \frac{\left(\frac{a}{2}\right)^2}{\left(a\right)^2}$$

$$I_{\text{removed}} = \frac{I_0}{16}$$

So, $I = I_0 - \frac{I_0}{16} = \frac{15I_0}{16}$

12. There are two long co-axial solenoids of same length *l*. the inner and outer coils have radii r_1 and r_2 and number of turns per unit length n_1 and n₂ respectively. The ratio of mutual inductance to the self-inductance of the inner-coil is :

(1)
$$\frac{n_2}{n_1} \cdot \frac{r_2^2}{r_1^2}$$
 (2) $\frac{n_2}{n_1} \cdot \frac{r_1}{r_2}$ (3) $\frac{n_1}{n_2}$ (4) $\frac{n_2}{n_1}$
Ans. (4)
Sol. $M = \mu_0 n_1 n_2 \pi r_1^2$
 $L = \mu_0 n_1^2 \pi r_1^2$
 $\Rightarrow \frac{M}{L} = \frac{n_2}{n_1}$

A rigid diatomic ideal gas undergoes an adiabatic process at room temperature,. The relation between temperature and volume of this process is $TV^x = constant$, then x is :

(1)
$$\frac{5}{3}$$
 (2) $\frac{2}{5}$ (3) $\frac{2}{3}$ (4) $\frac{3}{5}$

Ans. (2)

13.

Sol. For adiabatic process : $TV^{\gamma-1}$ = constant

For diatomic process : $\gamma - 1 = \frac{7}{5} - 1$

$$\therefore x = \frac{2}{5}$$

14. The gas mixture constists of 3 moles of oxygen and 5 moles of argon at temperature T. Considering only translational and rotational modes, the total inernal energy of the system is: (1) 12 RT (2) 20 RT (3) 15 RT (4) 4 RT 5)

Sol.
$$U = \frac{f_1}{2}n_1RT + \frac{f_2}{2}n_2RT$$
$$= \frac{5}{2}(3RT) + \frac{3}{2} \times 5RT$$
$$U = 15RT$$

15. In a Young's double slit experiment, the path different, at a certain point on the screen,

between two interfering waves is $\frac{1}{8}$ th of wavelength. The ratio of the intensity at this

point to that at the centre of a bright fringe is close to : (1) 0.94 (2) 0.74 (3) 0.85 (4) 0.80

Ans. (3)

Sol. $\Delta x = \frac{\lambda}{2}$

$$\Delta \phi = \frac{(2\pi)}{\lambda} \frac{\lambda}{8} = \frac{\pi}{4}$$
$$I = I_0 \cos^2\left(\frac{\pi}{8}\right)$$
$$\frac{I}{I_0} = \cos^2\left(\frac{\pi}{8}\right)$$

16. If the deBronglie wavelength of an electron is equal to 10^{-3} times the wavelength of a photon of frequency 6×10^{14} Hz, then the speed of electron is equal to : (Speed of light = 3×10^8 m/s Planck's constant = 6.63×10^{-34} J.s Mass of electron = 9.1×10^{-31} kg) (1) 1.45×10^6 m/s (2) 1.7×10^6 m/s (3) 1.8×10^6 m/s (4) 1.1×10^6 m/s Ans. (1) Sol. $\frac{h}{mv} = 10^{-3} \left(\frac{3 \times 10^8}{6 \times 10^{14}} \right)$

$$v = \frac{6.63 \times 10^{-34} \times 6 \times 10^{14}}{9.1 \times 10^{-31} \times 3 \times 10^5}$$
$$v = 1.45 \times 10^6 \text{ m/s}$$

17. A slab is subjected to two forces \vec{F}_1 and \vec{F}_2 of same magnitude F as shown in the figure. Force \vec{F}_2 is in XY-plane while force F_1 acts along z-axis at the point $(2\vec{i}+3\vec{j})$. The moment of these forces about point O will be :



- 18. A satellite is revolving in a circular orbit at a height h from the earth surface, such that h << R where R is the radius of the earth. Assuming that the effect of earth's atmosphere can be neglected the minimum increase in the speed required so that the satellite could escape from the gravitational field of earth is :
 - (1) $\sqrt{gR} \sqrt{2} 1$ (2) $\sqrt{2gR}$

(3)
$$\sqrt{gR}$$

Ans. (1)

- **Sol.** $v_0 = \sqrt{g(R+h)} \approx \sqrt{gR}$ $v_e = \sqrt{2g(R+h)} \approx \sqrt{2gR}$ $\Delta v = v_e - v_0 = \left(\sqrt{2} - 1\right)\sqrt{gR}$
- In an experiment electrons are accelerated, 19. from rest, by applying a voltage of 500 V. Calculate the radius of the path if a magnetic field 100 mT is then applied. [Charge of the electron = 1.6×10^{-19} C Mass of the electron = 9.1×10^{-31} kg] (1) 7.5×10^{-4} m (2) 7.5×10^{-3} m (4) 7.5×10^{-2} m (3) 7.5 m

Ans. (1)

Sol.
$$r = \frac{\sqrt{2mk}}{eB} = \frac{\sqrt{2me\Delta v}}{eB}$$

 $r = \sqrt{\frac{2m}{e} \cdot \Delta v} = \sqrt{\frac{2 \times 9.1 \times 10^{-31}}{1.6 \times 10^{-19}}} (500)$

В

r =
$$\frac{\sqrt{\frac{9.1}{0.16} \times 10^{-10}}}{10^{-1}} = \frac{3}{.4} \times 10^{-4} = 7.5 \times 10^{-4}$$

 100×10^{-3}

A particle undergoing simple harmonic motion 20. has time dependent displacement given by $x(t) = A \sin \frac{\pi t}{90}$. The ratio of kinetic to potential energy of this particle at t = 210 s will be :

(1) 2 (2)
$$\frac{1}{9}$$
 (3) 3 (4) 1

Ans. (3)

Sol. $k = \frac{1}{2}m\omega^2 A^2 \cos^2 \omega t$ $U = \frac{1}{2}m\omega^2 A^2 \sin^2 \omega t$ $\frac{k}{U} = \cot^2 \omega t = \cot^2 \frac{\pi}{90} (210) = \frac{1}{3}$ Hence ratio is 3 (most appropriate) 21. Ice at -20° C is added tp 50 g of water at 40° C. When the temperature of the mixture reaches 0°C, it is found that 20 g of ice is still unmelted. The amount of ice added to the water was close to (Specific heat of water = $4.2 \text{ J/g/}^{\circ}\text{C}$) Specific heat of Ice = $2.1 \text{ J/g/}^{\circ}\text{C}$ Heat of fusion of water at $0^{\circ}C = 334 \text{ J/g}$ (1) 50 g (2) 40 g (3) 60 g (4) 100 g

Ans. (2)

Ans.

Sol. Let amount of ice is m gm. According to principal of calorimeter heat taken by ice = heat given by water $\therefore 20 \times 2.1 \times m + (m - 20) \times 334$ $= 50 \times 4.2 \times 40$ 376 m = 8400 + 6680

$$m = 40.1 \text{ g}$$

22. In the figure shown below, the charge on the left plate of the 10 μ F capacitor is -30 μ C. The charge on the right plate of the 6 μ F capacitor is :



(1)
$$-18 \ \mu C$$

(3) $+12 \ \mu C$
(4) $+18 \ \mu C$
(4)



6µF & 4µF are in parallel & total charge on this combination is 30 µC

:. Charge on 6µF capacitor = $\frac{6}{6+4} \times 30$

 $= 18 \ \mu C$ Since charge is asked on right plate therefore is +18µC Correct answer is (4)





- Sol. Since voltage across zener diode must be less than 10V therefore it will not work in breakdown region, & its resistance will be infinite & current through it = 0
 - \therefore correct answer is (4)
- 24. The variation of refractive index of a crown glass thin prism with wavelength of the incident light is shown. Which of the following graphs is the correct one, if D_m is the angle of minimum deviation?





Sol. Since $D_m = (\mu - 1)A$

& on increasing the wavelength, μ decreases & hence D_m decreases. Therefore correct answer is (2)

25. The resistance of the meter bridge AB in the given figure is 4 Ω . With a cell of emf $\varepsilon = 0.5$ V and rheostat resistance $R_h = 2 \Omega$ the null point is obtained at some point J. When the cell is replaced by another one of emf $\varepsilon = \varepsilon_2$ the same null point J is found for $R_h = 6 \Omega$. The emf ε_2 is;



Ans. (3)

Sol. Potential gradient with $R_h = 2\Omega$

is
$$\left(\frac{6}{2+4}\right) \times \frac{4}{L} = \frac{dV}{dL}$$
; L = 100 cm

Let null point be at $\ell\ cm$

thus
$$\varepsilon_1 = 0.5 \text{V} = \left(\frac{6}{2+4}\right) \times \frac{4}{\text{L}} \times \ell \qquad \dots (1)$$

Now with $R_h = 6\Omega$ new potential gradient is

$$\left(\frac{6}{4+6}\right) \times \frac{4}{L}$$
 and at null point

$$\left(\frac{6}{4+6}\right)\left(\frac{4}{L}\right) \times \ell = \varepsilon_2 \qquad \dots (2)$$

dividing equation (1) by (2) we get

$$\frac{0.5}{\epsilon_2} = \frac{10}{6} \text{ thus } \epsilon_2 = 0.3$$

26. The given graph shows variation (with distance r from centre) of :



- (1) Potential of a uniformly charged sphere
- (2) Potential of a uniformly charged spherical shell
- (3) Electric field of uniformly charged spherical shell

(4) Electric field of uniformly charged sphere

Ans. (2)

Sol. Conceptual

27. Two equal resistance when connected in series to a battery, consume electric power of 60 W. If these resistances are now connected in parallel combination to the same battery, the electric power consumed will be :

(1) 60 W	(2) 240 W
(3) 30 W	(4) 120 W

Ans. (2)

Sol. In series condition, equivalent resistance is 2R

thus power consumed is $60W = \frac{\epsilon^2}{2R}$

In parallel condition, equivalent resistance is R/ 2 thus new power is

$$P' = \frac{\epsilon^2}{(R/2)}$$

or P' = 4P = 240W

28. An object is at a distance of 20 m from a convex lens of focal length 0.3 m. The lens forms an image of the object. If the object moves away from the lens at a speed of 5 m/s, the speed and direction of the image will be :
(1) 0.92 × 10⁻³ m/s away from the lens
(2) 2.26 × 10⁻³ m/s away from the lens
(3) 1.16 × 10⁻³ m/s towards the lens
(4) 3.22 × 10⁻³ m/s towards the lens
Ans. (3)

Sol. From lens equation

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

$$\frac{1}{v} - \frac{1}{(-20)} = \frac{1}{(.3)} = \frac{10}{3}$$

$$\frac{1}{v} = \frac{10}{3} - \frac{1}{20}$$

$$\frac{1}{v} = \frac{197}{60}; v = \frac{60}{197}$$

$$m = \left(\frac{v}{u}\right) = \frac{\left(\frac{60}{197}\right)}{20}$$

velocity of image wrt. to lens is given by $v_{I/L} = m^2 v_{O/L}$

direction of velocity of image is same as that of object

 $v_{O/L} = 5 \text{ m/s}$

$$v_{\text{tr.}} = \left(\frac{60 \times 1}{197 \times 20}\right)^2 (5)$$
= 1.16 × 10⁻³ m/s towards the lens
29. A body of mass 1 kg falls freely from a height for 0 m on a platform of mass 3 kg which is mounted on a spring having spring constant k = 1.25 × 100 N/m. The body sticks to the platform and the spring's maximum compression is found to be x. Given that g = 10 ms⁻², the value of x will be close to :
(1) 4 cm
(2) 8 cm
(3) 80 cm
(4) 40 cm
Ans. (1)
Sol. Velocity of 1 kg block just before it collides with 3kg block = $\sqrt{2gh} - \sqrt{2000} \text{ m/s}$
Applying momenum conversation just before and just after collision.
 $1 \times \sqrt{2000} = 4v \Rightarrow v = \frac{\sqrt{2000}}{4} \text{ m/s}$
initial compression of spring
 $1.25 \times 10^{v} \text{ kp} = 70 = x_{v} = 0$
applying work dangy theorem, $W_{v} + W_{w} = 2MGH$
 $\Rightarrow 40 \times x + \frac{1}{2} \times 1.25 \times 10^{6} (0^{2} - x^{2})$
 $= 0 - \frac{1}{2} x 4 xv^{2}$
solving x ≈ 4 cm

TEST PAPER OF JEE(MAIN) EXAMINATION – 2019 (Held On Friday 11th JANUARY, 2019) TIME : 9 : 30 AM To 12 : 30 PM CHEMISTRY

1. For the cell $Zn(s) | Zn^{2+}(aq) || M^{x+}(aq) | M(s)$, different half cells and their standard electrode potentials are given below :

$M^{x+}(a\alpha/M(s))$	Au ³⁺ (aq)/	Ag ⁺ (aq)/	Fe ³⁺ (aq)/	Fe ²⁺ (aq)/
wi (aq/ wi(3)	Au(s)	Ag(s)	$\mathrm{Fe}^{2+}(\mathrm{aq})$	Fe(s)
$E^{o}_{M^{x+}/M^{(v)}}$	1.40	0.80	0.77	-0.44

If $E_{Zn^{2+}/Zn}^{o} = -0.76 V$, which cathode will give a

mximum value of E_{cell}^{o} per electron transferred ?

(1) Fe^{3+} / Fe^{2+}	(2) Ag ⁺ / Ag
(3) Au ³⁺ / Au	(4) Fe ²⁺ / Fe

Ans. (2)

2. The correct match between items-I and II is :

Item-I	Item-II
(Mixture)	(Separation method)
(A) H_2O : Sugar	(P) Sublimation
(B) H ₂ O : Aniline	(Q) Recrystallization
(C) H ₂ O : Toluene	(R) Steam distillation
	(S) Differential
	extraction

-R. B-P. C-S

A-Q, B-R, C-P

- (1) A-Q, B-R, C-S
- (3) A-S, B-R, C-P
- Ans. (1)
- Sol. (Mixture)(Seperation method) H_2O : SugarRecrystallization H_20 : Aniline \Rightarrow Steam distillation
 - H_2O : Toluene \Rightarrow Differential extraction
- 3. If a reaction follows the Arrhenius equation, the

plot lnk vs $\frac{1}{(RT)}$ gives straight line with a

gradient (-y) unit. The energy required to activate the reactant is :

(1) y unit	(2) –y unit

- (3) yR unit (4) y/R unit
- Ans. (1)

- **4.** The concentration of dissolved oxygen (DO) in cold water can go upto :
 - (1) 10 ppm (2) 14 ppm
 - (3) 16 ppm (4) 8 ppm

Ans. (1)

- **Sol.** In cold water, dissolved oxygen (DO) can reach a concentration upto 10 ppm
- 5. The major product of the following reaction is:



- (c) Dihydrogen is stored in tanks of metal alloys like NaNi₅
- (d) On combustion, values of energy released per gram of liquid dihydrogen and LPG are 50 and 142 kJ, respectively
- (1) b and d only (2) a, b and c only
- (3) b, c and d only (4) a and c only

Ans. (2)

6.

Sol. Option (a), (b) & (c) are correct answer (NCERT THEORY BASED)



12.	Which compound(s) out of	of the following is/are not	15.	Consider the reaction,	
	aromatic ?			$N_2(g) + 3H_2(g) \longrightarrow 2I$	$NH_3(g)$
	$\nabla \bigcirc ($			The equilibrium constant K_{p} . If pure ammonia is left pressure of ammonia at C_{p}	t of the above reaction is t to dissociate, the partial equilibrium is given by
	\oplus \oplus	$\Theta \sim$		(Assume that $P_{NH_3} \ll P_{tot}$	al at equilibrium)
	(A) (B)	(C) (D)		(1) $\frac{3^{\frac{3}{2}} K_{P}^{\frac{1}{2}} P^{2}}{3^{\frac{1}{2}} K_{P}^{\frac{1}{2}} P^{2}}$	(2) $\frac{3^{\frac{3}{2}} K_{P}^{\frac{1}{2}} P^{2}}{3^{\frac{1}{2}} K_{P}^{\frac{1}{2}} P^{2}}$
	(1) C and D	(2) B, C and D		4	16
	(3) A and C	(4) B		(2) $K^{\frac{1}{2}}_{\frac{1}{2}} P^2$	(1) $K_{p}^{\frac{1}{2}} P^{2}$
Ans.	(2)			$(3) \frac{-1}{16}$	(4) $\frac{p}{4}$
Sol.	out of the given options Hence (B) (C) and (D) :	only $\stackrel{\textcircled{\bullet}}{}$ is aromatic.	Ans. 16.	(2) Match the ores(Colum (column B) : <i>Column-A</i>	n A) with the metals <i>Column-B</i>
10	Thence (D), (C) and (D)			Ores	Metals
13.	The correct match betwe	een Item(I) and Item(II)		(I) Siderite (II) Kaolinite	(a) Zinc (b) Copper
	IS.	Itom_II		(III) Malachite	(c) Iron
	(A) Nortchindrone	(D) Anti biotic		(1V) Calamine (1) I-b : II-c : III-d : IV	(d) Aluminium
	(A) Nontenindrone	(P) Anti-blouc		(2) I-c ; II-d ; III-a ; IV	-b
	(B) Ofloxacin	(Q) Anti-fertility	\sim	(3) I-c; II-d; III-b; IV (4) La \cdot II b \cdot III c \cdot IV	-a d
	(C) Equanil	(R) Hypertension	Ans.	(3)	-u
		(S) Analgesics	Sol.	Siderite : FeCO ₃	
	(1) A-R, B-P, C-S	(2) A-Q, B-P, C-R		Kaolinite : $Al_2(OH)_4Si_2O$	5
	(3) A-R, B-P, C-R	(4) A-Q, B-R, C-S		Malachite : $Cu(OH)_2$.Cu	
Ans.	(2)	5	17.	The correct order of the a	tomic radii of C, Cs, Al
Sol.	(A) Norethindrone – Ant	ifertility		and S is :	
	(B) Ofloaxacin – Anti-Bi	otic		(1) $S < C < AI < Cs$ (3) $C < S < Cs < AI$	(2) $S < C < Cs < Al$ (4) $C < S < Al < Cs$
	(C) Equanil – Hypertensi	on (traiquilizer)	Ans.	(4)	(4) C < 5 < 711 < C5
14.	Heat treatment of muscula	ar pain involves radiation		In a period	AR J
	of wavelength of about 9	900 nm. Which spectral			
	line of H-atom is suitabl	e for this purpose?	Sol.	(AK-Ator	nic radius)
	$[R_{\rm H} = 1 \times 10^5 \text{ cm}^{-1}]$,	$h = 6.6 \times 10^{-34} Js,$		AR↑	
	$c = 3 \times 10^8 \text{ ms}^{-1}]$			Atomic radii order : C <	S < Al < Cs
	(1) Paschen, $5 \rightarrow 3$	(2) Paschen, $\infty \rightarrow 3$		Atomic radius of C : 170) pm
	(3) Lyman, $\infty \rightarrow 1$	(4) Balmer, $\infty \rightarrow 2$		Atomic radius of S : 180	pm 4 pm
Ans.	(2)			Atomic radius of Cs · 30	4 pm 00 pm
					~ Pm

18. Match the metals (Column I) with the coordination compound(s) / enzyme(s) (Column II)

Column-I	Column-II
Metals	Coordination compound(s) / Enzyme(s)
(A)Co	(i) Wilkinson catalyst
(B)Zn	(ii) Chlorophyll
(C) Rh	(iii) Vitamin B ₁₂
(D) Mg	(iv) Carbonic anhydrase
(1) A-ii ; B-i ; C-iv ;	D-iii
(2) A-iii ; B-iv ; C-i	; D-ii
(3) A-iv ; B-iii ; C-i	; D-ii
(4) A-i ; B-ii ; C-iii ;	D-iv
(2)	
(1) XX 7'11 1 . 1	

- Ans. (2)
- **Sol.** (i) Wilkinson catalyst : $RhCl(PPh_3)_3$
 - (ii) Chlorophyll : C₅₅H₇₂O₅N₄Mg
 - (iii) Vitamin B₁₂(also known as
 - cyanocobalamin) contain cobalt.
 - (iv) Carbonic anhydrase contains a zinc ion.
- **19.** A 10 mg effervescent tablet contianing sodium bicarbonate and oxalic acid releases 0.25 ml of CO_2 at T = 298.15 K and p = 1 bar. If molar volume of CO_2 is 25.0 L under such condition, what is the percentage of sodium bicarbonate in each tablet ? [Molar mass of NaHCO₃ = 84 g mol⁻¹]
 - (1) 16.8
 - (3) 0.84

Ans. (2)

Sol.

Moles of CO₂ evolved =
$$\frac{0.25}{25 \times 10^3} = 10^{-5}$$

 \therefore moles of NaHCO₃ = 10^{-5}

) 33.6

= 0.84 × 10⁻³ o

:. % by weight =
$$\frac{0.84}{10} \times 100$$

= 8.4 %

20. The major product of the following reaction is :



Two blocks of the same metal having same mass and at temperature T_1 and T_2 , respectively. are brought in contact with each other and allowed to attain thermal equilibrium at constant pressure. The change in entropy, ΔS , for this process is :

(1)
$$2C_{p} \ln \left(\frac{T_{1} + T_{2}}{4T_{1}T_{2}}\right)$$
 (2) $2C_{p} \ln \left[\frac{(T_{1} + T_{2})^{\frac{1}{2}}}{T_{1}T_{2}}\right]$

(3)
$$C_{P} \ln \left[\frac{(T_{1} + T_{2})^{2}}{4T_{1}T_{2}} \right]$$
 (4) $2C_{P} \ln \left[\frac{T_{1} + T_{2}}{2T_{1}T_{2}} \right]$

Ans. (3)

21.

Final temperature =
$$\frac{T_1 + T_2}{2}$$
, let $T_2 > T_1$

 $\therefore \quad dS = \frac{dq}{T} = \frac{C_P dT}{T}$ $\therefore \quad \Delta S = C_P \ln\left(\frac{T_f}{T_i}\right)$ $\therefore \quad \Delta S_{total} = C_P \ln\left(\frac{T_1 + T_2}{2T_1}\right) + C_P \ln\left(\frac{T_1 + T_2}{2T_2}\right)$ $= C_P \ln\left[\frac{(T_1 + T_2)^2}{4T_1T_2}\right]$

(1) SiCl ₄ (2) SnCl ₄ (3) PbCl ₄ (4) CCl ₄ Ans. (4) Sol. CCl ₄ cannot get hydrolyzed due to the absence of vacant orbital at carbon atom. 23. For the chemical reaction $X \longrightarrow Y$, the standard reaction Gibbs energy depends on temperature T (in K) as : $\Delta_{i}C^{\alpha}$ (in kJ mol ⁻¹) = 120 - $\frac{3}{8}T$ The major component of the reaction mixture at T is : (1) X if T = 315 K (2) X if T = 300 K (3) Y if T = 300 K (4) Y if T = 280 K Ans. (1) Sol. a - $\frac{Z \times M}{N \times a^3}$ $9 \times 10^3 = \frac{2}{(200 \times 2^2 \times 10^{-12})^3 6 \times 10^{23}}$ M = 0.03 kotomoe 24. The freezing point of a diluted milk sample is found to be -0.2°C, while it should have been -0.5°C for pure milk. How much water has been added to pure milk. How much water has been added to pure milk. How much water has been added to pure milk. (3) 3 cups of water to 3 cups of pure milk (3) Cup of water to 3 cups of pure milk (4) I cup of water to 3 cups of pure milk (3) I cup of water to 2 cups of pure milk (4) I cup of water to 2 cups of pure milk (3) Cup of water to 2 cups of pure milk (4) I cup of water to 2 cups of pure milk (3) Puint (4) Hair cream Ans. (2) 5 5 5 5 5 5 5 5 5 5 5 5 5	22.	The chloride that CANNOT get hydrolysed is :	Sol.		
(3) PECl ₄ (4) CCl ₄ Ans. (4) Sol. CCl ₄ cannot get hydrolyzed due to the absence of vacant orbital at carbon atom. 23. For the chemical reaction $X \Longrightarrow Y$, the standard reaction Gibbs energy depends on temperature T (in K) as : ΔG° (in kl mol ⁻¹) = $120 - \frac{3}{8}T$ The major component of the reaction mixture at T is : (1) X if T = 315 K (2) X if T = 300 K (3) Y if T = 300 K (4) Y if T = 280 K Ans. (1) Sol. $a = \frac{Z \times M}{N \times a^3}$ $9 \times 10^3 = \frac{2}{(200 - 2 - 10^{-12})^3 6 \times 10^{23}}$ M = 0.03 kg/mote 24. The freezing point of a diluted milk sample is found to be -0.2° C, while it should have been -0.5° Cfor pure milk. How much water has been added to pure milk. How much water to 3 cups of pure milk (2) 1 cup of water to 3 cups of pure milk (3) 2 cups of water to 3 cups of pure milk (4) 1 cup of water to 2 cups of pure milk (4) 1 cup of water to 2 cups of pure milk (3) 2 cups of water to 2 cups of pure milk (4) 1 cup of water to 2 cups of pure milk (5) 3 cups of water to 2 cups of pure milk (4) 1 cup of water to 2 cups of pure milk (5) 3 cups of water to 2 cups of pure milk (6) 1 cup of water to 2 cups of pure milk (6) 1 cup of water to 2 cups of pure milk (6) 1 cup of water to 2 cups of pure milk (6) 1 cup of water to 2 cups of pure milk (6) 1 cup of water to 2 cups of pure milk (6) 1 cup of water to 2 cups of pure milk (7) 1 cup of water to 2 cups of pure milk (8) 1 cup of water to 2 cups of pure milk (9) 1 cup of water to 2 cups of pure milk (1) 1 Butter (2) Gem stones (3) Paint (4) Hair cream Ans. (2) (2) Col CH (2) CH		(1) SiCl_4 (2) SnCl_4	0.5 w ₁		
Ans. (4) Sol. CCl ₄ cannot get hydrolyzed due to the absence of vacant orbital at carbon atom. 23. For the chemical reaction $X \longrightarrow Y$, the standard reaction Gibbs energy depends on temperature T (in K) as : $\Delta_{C}G^{\circ}$ (in kJ mol ⁻¹) = $120 - \frac{3}{8}T$ The major component of the reaction mixture at T is : (1) X if T = 315 K (2) X if T = 350 K (3) Y if T = 300 K (4) Y if T = 280 K Ans. (1) Sol. $a = \frac{Z \times M}{N \times a^3}$ $9 \times 10^3 = \frac{2 \times M}{(200 + 2 \times 40^{-12})^3 6 \times 10^{23}}$ M = 0.03 kg/mole 24. The freezing point of a diluted milk sample is found to be $-0.2^{\circ}C$, while it should have been $-0.5^{\circ}C$ for pure milk. How much water has been added to pure milk. (2) 1 cup of water to 3 cups of pure milk (3) 3 cups of water to 3 cups of pure milk (4) 1 cup of water to 3 cups of pure milk (3) 2 cups of water to 2 cups of pure milk (4) 1 cup of water to 2 cups of pure milk Ans. (3) Ans. (2) $Box(()^{NH}, \frac{NaNO_{1}}{H_{1}O} HOCC + O^{OH}$ $Hooc + O^{2/C}, While it should have been -0.5^{\circ}C for pure milk. How much water has been added in the follows of the solid sol is :(1) 2 cups of water to 3 cups of pure milk(3) a cups of water to 2 cups of pure milk(4) 1 cup of water to 2 cups of pure milkAns. (3)Hooc$		(3) $PbCl_4$ (4) CCl_4	$\Rightarrow \overline{0.2} = \overline{w_1}$		
Sol. CCl ₄ cannot get hydrolyzed due to the absence of vacant orbital at carbon atom. 23. For the chemical reaction $X \implies Y$, the standard reaction Gibbs energy depends on temperature T (in K) as : $\Delta_{G^{\alpha}} (\text{in kJ mol}^{-1}) = 120 - \frac{3}{8}T$ The major component of the reaction mixture at T is : (1) X if T = 315 K (2) X if T = 300 K (3) Y if T = 300 K (4) Y if T = 280 K Ans. (1) Sol. $a = \frac{Z \times M}{N \times a^3}$ (1) $Sol = \frac{Z \times M}{(200 \times 2 \times 10^{-12})^3 6 \times 10^{23}}$ M = 0.05 keymote 4. The freezing point of a diluted milk sample is fount to be -0.2° C, while it should have been -0.5° C for pure milk How much water has been added to pure milk. How much water has been added to pure milk. How much water has been added to pure milk (2) I cup of water to 3 cups of pure milk (3) 3 cups of water to 3 cups of pure milk (4) 1 cup of water to 3 cups of pure milk (3) 2 cups of diluted milk sample is found to following the sample is found to pure milk (3) 3 cups of water to 2 cups of pure milk (4) 1 cup of water to 2 cups of pure milk (4) 1 cup of water to 2 cups of pure milk (3) 2 cups of solid sol is : (3) Paint (4) Hair cream Ans. (2) 27. An example of solid sol is : (3) Paint (4) Hair cream Ans. (2) (4) Substance (2) Cups of pure milk (5) Found the cup of water to 2 cups of pure milk (6) 1 cup of water to 2 cups of pure milk (7) 1 cup of water to 2 cups of pure milk (8) 1 cup of water to 2 cups of pure milk (4) 1 cup of water to 2 cups of pure milk (5) Paint (4) Hair cream Ans. (2)	Ans.	(4)	$\Rightarrow \frac{W'_1}{W'_1} = \frac{5}{2}$		
23. For the chemical reaction $X \longrightarrow Y$, the standard reaction Gibbs energy depends on temperature T (in K) as : $\Delta_{1}G^{\alpha} (in kJ mol^{-1}) = 120 - \frac{3}{8}T$ The major component of the reaction mixture at T is : (1) X if T = 315 K (2) X if T = 315 K (2) X if T = 300 K (3) Y if T = 300 K (4) Y if T = 280 K Ans. (1) Sol. $a = \frac{Z \times M}{N \times a^{3}}$ $9 \times 10^{3} = \frac{200 \sqrt{Z} \times 10^{-1}}{(200 \sqrt{Z} \times 10^{-1})^{3} 6 \times 10^{23}}$ M = 0.03 kg/mole 24. The freezing point of a diluted milk sample is found to be -0.2°C, while it should have been -0.5°C for pure milk. How much water has been added to pure milk. How much water has been added to pure milk. How much water has been added to pure milk. How much water has been added to pure milk. How much water to 3 cups of pure milk (3) 3 cups of water to 3 cups of pure milk (4) 1 cup of water to 2 cups of pure milk (5) Cup of water to 2 cups of pure milk (4) 1 cup of water to 2 cups of pure milk (5) Paint (4) Hair cream Ans. (2) (5) Paint (4) Hair cream Ans. (2)	Sol.	CCl_4 cannot get hydrolyzed due to the absence of vacant orbital at carbon atom.	w ₁ 2 2 cups of p overall 5 cup	ure milk mixed s of diluted mill	d with 3 cups of water k.
(d) Y if T = 280 K Ans. (1) Sol. $a = \frac{Z \times M}{N \times a^{3}}$ $9 \times 10^{3} = \frac{200 \sqrt{Z} \times 10^{-12}}{(200 \sqrt{Z} \times 10^{-12})^{3} 6 \times 10^{23}}$ $M = 0.03$ kg/more 24. The freezing point of a diluted milk sample is found to be -0.2° C, while it should have been -0.5° C for pure milk. How much water has been added to pure milk. How much water has been added to pure milk. How much water has been added to pure milk to make the diluted sample ? (1) 2 cups of water to 3 cups of pure milk (2) 1 cup of water to 3 cups of pure milk (3) 3 cups of water to 2 cups of pure milk (4) 1 cup of water to 2 cups of pure milk (5) 2 cups of water to 2 cups of pure milk (6) 1 cup of water to 2 cups of pure milk (7) An example of solid sol is : (1) Butter (2) Gem stones (3) Paint (4) Hair cream Ans. (2) 5	23.	For the chemical reaction $X \rightleftharpoons Y$, the standard reaction Gibbs energy depends on temperature T (in K) as : $\Delta_r G^o (in kJ mol^{-1}) = 120 - \frac{3}{8}T$ The major component of the reaction mixture at T is : (1) X if T = 315 K (2) X if T = 350 K (3) Y if T = 300 K	25. A solid face cet $200\sqrt{2}$ solid ? (Avogać (1) 0.02 (3) 0.43: Ans. (2) 26. The poly is :	having density of ntred cubic cry pm. What is the lro constant $\cong 6$ 16 kg mol ⁻¹ 20 kg mol ⁻¹	of 9×10^3 kg m ⁻³ forms ystals of edge length he molar mass of the 5×10^{23} mol ⁻¹ , $\pi \approx 3$) (2) 0.0305 kg mol ⁻¹ (4) 0.0432 kg mol ⁻¹
Ans. (1) Sol. $a = \frac{Z \times M}{N \times a^{3}}$ $9 \times 10^{3} = \frac{200 \times 2 \times 10^{-12}}{(200 \times 2 \times 10^{-12})^{3} 6 \times 10^{23}}$ $M = 0.03 \text{ kg/mote}$ (1) $\begin{bmatrix} 0 \\ C \\ -(CH)_{1} \\ - \\ - \\ - \\ - \\ - \\ - \\ - \\ - \\ - \\ $		(4) Y if $T = 280 \text{ K}$			I_2 (i) NaNO ₂ /H ₃ O ⁺
Sol. $a = \frac{Z \times M}{N \times a^{3}}$ $9 \times 10^{3} = \frac{200 \times 5^{2} \times 10^{-12}}{(200 \times 5^{2} \times 10^{-12})^{3} 6 \times 10^{23}}$ $M = 0.03 \text{ kymote}$ (1) $\begin{bmatrix} 0 \\ C \\ (CH_{1})_{1} - 0 \end{bmatrix}_{n}$ (2) $\begin{bmatrix} 0 \\ (CH_{2})_{1} - 0 - 1 \end{bmatrix}_{n}$ (3) $\begin{bmatrix} H_{NC}(CH_{1})_{1} - 0 - 1 \end{bmatrix}_{n}$ (4) $\begin{bmatrix} 0 \\ OC(CH_{1})_{1} - 0 - 1 \end{bmatrix}_{n}$ (4) $\begin{bmatrix} 0 \\ OC(CH_{1})_{1} - 0 - 1 \end{bmatrix}_{n}$ (5) $H_{NC}(CH_{1})_{1} - 0 - 1 \end{bmatrix}_{n}$ (6) $\begin{bmatrix} 0 \\ C \\ (CH_{1})_{1} - 0 - 1 \end{bmatrix}_{n}$ (7) $H_{12} \cdot \frac{NaNO_{2}}{H_{1}O^{2}} + H_{10}O^{2} + H_{$	Ans.	(1)	HOOC /	\checkmark \checkmark	(ii) Polymerisation
 24. The freezing point of a diluted milk sample is found to be -0.2°C, while it should have been -0.5°C for pure milk. How much water has been added to pure milk to make the diluted sample ? (1) 2 cups of water to 3 cups of pure milk (2) 1 cup of water to 3 cups of pure milk (3) 3 cups of water to 2 cups of pure milk (4) 1 cup of water to 2 cups of pure milk (3) 27. An example of solid sol is : (1) Butter (2) Gem stones (3) Paint (4) Hair cream Ans. (3) 	301.	$a = \frac{Z \times M}{N \times a^3}$ 9×10 ³ = $\frac{4 \times M}{(200 \times \sqrt{2} \times 10^{-12})^3 6 \times 10^{23}}$ M = 0.03 kg/mole	$(1) \begin{bmatrix} 0\\ -C\\ 0\\ (2) \begin{bmatrix} 0\\ 0\\ (3) \end{bmatrix} \begin{bmatrix} -H\\ (4) \end{bmatrix} \begin{bmatrix} 0\\ 0\\ Ans. (2)\\ Sol. \end{bmatrix}$	$\begin{array}{c} H \\ -(CH_{2})_{4}-N \\ n \\ -(CH_{2})_{4}-C \\ n \\ NC(CH_{2})_{4}-C \\ -N \\ n \\ C(CH_{2})_{4}-C \\ n \\ n \end{array}$	1
 (1) 2 cups of water to 3 cups of pure milk (2) 1 cup of water to 3 cups of pure milk (3) 3 cups of water to 2 cups of pure milk (4) 1 cup of water to 2 cups of pure milk Ans. (3) 27. An example of solid sol is : (1) Butter (2) Gem stones (3) Paint (4) Hair cream Ans. (2) 5	24.	The freezing point of a diluted milk sample is found to be -0.2° C, while it should have been -0.5° C for pure milk. How much water has been added to pure milk to make the diluted sample ?	ноос	\sim NH ₂ $\frac{\text{NaNe}}{\text{H}_3\text{O}^+}$	$\begin{array}{c} O_{2} \\ \hline \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ $
(3) 3 cups of water to 2 cups of pure milk (4) 1 cup of water to 2 cups of pure milk Ans. (3) (1) Butter (2) Gem stones (3) Paint (4) Hair cream Ans. (2) 5		(1) 2 cups of water to 3 cups of pure milk(2) 1 cup of water to 3 cups of pure milk	27. An exar	nple of solid sol	is :
Ans. (3) Ans. (2) 5		(3) 3 cups of water to 2 cups of pure milk(4) 1 cup of water to 2 cups of pure milk	(1) Butt (3) Pain	er t	(2) Gem stones (4) Hair cream
5	Ans.	(3)	Ans. (2)	u.	(7) fran cream
					5

- **28.** Peroxyacetyl nitrate (PAN), an eye irritant is produced by :
 - (1) Acid rain
 - (3) Classical smog (4) Organic waste

(2) Photochemical smog

Schor

- Ans. (2)
- **Sol.** Photochemical smog produce chemicals such as formaldehyde, acrolein and peroxyacetyl nitrate (PAN).
- 29. NaH is an example of :
 (1) Electron-rich hydride (2) Molecular hydride
 (3) Saline hydride (4) Metallic hydride
- Ans. (3)
- **Sol.** NaH is an example of ionic hydride which is also known as saline hydride.
- **30.** The amphoteric hydroxide is :
 - (1) $Ca(OH)_2$ (2) $Be(OH)_2$
 - (3) $Sr(OH)_2$ (4) $Mg(OH)_2$
- Ans. (2)
- **Sol.** $Be(OH)_2$ is amphoteric in nature while rest all alkaline earth metal hydroxide are basic in nature.

reoler

TEST PAPER OF JEE(MAIN) EXAMINATION – 2019 (Held On Friday 11th JANUARY, 2019) TIME : 9 : 30 AM To 12 : 30 PM MATHEMATICS

		-	
	$\begin{pmatrix} 0 & 2q & r \end{pmatrix}$	3.	The outcome of each of 30 items was observed;
1.	Let $A = \begin{pmatrix} p & q & -r \\ p & -q & r \end{pmatrix}$. It $AA^{T} = I_{3}$, then $ p $		10 items gave an outcome $\frac{1}{2}$ – d each, 10 items
	is:		gave outcome $\frac{1}{2}$ each and the remaining
	(1) $\frac{1}{\sqrt{2}}$		10 items gave outcome $\frac{1}{2}$ + d each. If the
	(2) $\frac{1}{\sqrt{5}}$		variance of this outcome data is $\frac{4}{3}$ then $ d $
	(3) $\frac{1}{\sqrt{6}}$		equals :-
	(4) $\frac{1}{\sqrt{3}}$	Ans.	(1) 2 (2) $\frac{\sqrt{3}}{2}$ (3) $\frac{2}{3}$ (4) $\sqrt{2}$ (4)
Ans. Sol.	(1) A is orthogonal matrix	Sol.	Variance is independent of origin. So we shift
	$\Rightarrow 0^2 + p^2 + p^2 = 1 \Rightarrow p = \frac{1}{\sqrt{2}}$	\mathcal{N}	the given data by $\frac{1}{2}$.
2.	The area (in sq. units) of the region bounded by the curve $x^2 = 4y$ and the straight line	り	so, $\frac{10d^2 + 10 \times 0^2 + 10d^2}{30} - (0)^2 = \frac{4}{3}$
	x = 4y - 2 :-		$\Rightarrow d^2 = 2 \Rightarrow d = \sqrt{2}$
	$(1) \frac{5}{4}$	4.	The sum of an infinite geometric series with positive terms is 3 and the sum of the cubes of
	(2) $\frac{9}{8}$		its terms is $\frac{27}{19}$. Then the common ratio of this
	(3) $\frac{3}{4}$		series is : 2
	$(4) \frac{7}{2}$		(1) $\frac{4}{9}$ (2) $\frac{2}{9}$
Ans.	(2) 8		(3) $\frac{2}{3}$ (4) $\frac{1}{3}$
		Ans.	(3)
Sol.		Sol.	$\frac{a}{1-r} = 3 \qquad \dots (1)$
	$x = 4y - 2 & x^2 = 4y$ $\Rightarrow x^2 = x + 2 \Rightarrow x^2 - x - 2 = 0$ x = 2 - 1		$\frac{a^{3}}{1-r^{3}} = \frac{27}{19} \implies \frac{27(1-r)^{3}}{1-r^{3}} = \frac{27}{19}$
	$\int_{1}^{2} \left(x+2 + x^{2} \right) dx = 9$		$\Rightarrow 6r^2 - 13r + 6 = 0$ 2
	So, $\int_{-1} \left(\frac{1}{4} - \frac{1}{4} \right) dx = \frac{1}{8}$		\Rightarrow r = $\frac{-}{3}$ as r < 1
			1

Let $\vec{a} = \hat{i} + 2\hat{j} + 4\hat{k}$, $\vec{b} = \hat{i} + \lambda\hat{j} + 4\hat{k}$ and 5. 7. Let $f(x) = \begin{cases} -1, -2 \le x < 0 \\ x^2 - 1, 0 \le x \le 2 \end{cases}$ and $\vec{c} = 2\hat{i} + 4\hat{j} + (\lambda^2 - 1)\hat{k}$ be coplanar vectors. Then the non-zero vector $\vec{a} \times \vec{c}$ is : g(x) = |f(x)| + f(|x|). Then, in the interval (1) $-14\hat{i} - 5\hat{j}$ (2) $-10\hat{i} - 5\hat{j}$ (-2, 2), g is :-(1) differentiable at all points (3) $-10\hat{i} + 5\hat{j}$ (4) $-14\hat{i} + 5\hat{j}$ (2) not differentiable at two points (3) not continuous Ans. (3) (4) not differentiable at one point **Sol.** $\begin{bmatrix} \vec{a} & \vec{b} & \vec{c} \end{bmatrix} = 0$ Ans. (4) Sol. $|f(\mathbf{x})| = \begin{cases} 1 & , -2 \le \mathbf{x} < 0 \\ 1 - \mathbf{x}^2 & , 0 \le \mathbf{x} < 1 \\ \mathbf{x}^2 - 1 & , 1 \le \mathbf{x} \le 2 \end{cases}$ $\Rightarrow \begin{vmatrix} 1 & 2 & 4 \\ 1 & \lambda & 4 \\ 2 & 4 & \lambda^2 & 1 \end{vmatrix} = 0$ and $f(|\mathbf{x}|) = \mathbf{x}^2 - 1, \ \mathbf{x} \in [-2, \ 2]$ $\Rightarrow \lambda^3 - 2\lambda^2 - 9\lambda + 18 = 0$ $\Rightarrow \lambda^2(\lambda - 2) - 9(\lambda - 2) = 0$ Hence $g(x) = \begin{cases} x^2 , x \in [-2,0) \\ 0 , x \in [0,1) \\ 2(x^2 - 1) & x \in [1,2] \end{cases}$ $\Rightarrow (\lambda - 3)(\lambda + 3)(\lambda - 2) = 0$ $\Rightarrow \lambda = 2, 3, -3$ So, $\lambda = 2$ (as \vec{a} is parallel to \vec{c} for $\lambda = \pm 3$) It is not differentiable at x = 1Hence $\vec{a} \times \vec{c} = \begin{vmatrix} 1 & j & \kappa \\ 1 & 2 & 4 \\ 2 & 4 & 3 \end{vmatrix}$ Let $f : R \to R$ be defined by $f(x) = \frac{x}{1 + x^2}$, 8. $x \in R$. Then the range of f is : $= -10\hat{i} + 5\hat{j}$ (1) $(-1, 1) - \{0\}$ (2) $\left| -\frac{1}{2}, \frac{1}{2} \right|$ Let $\left(-2-\frac{1}{2}\right)$ $\frac{1y}{2}(i=\sqrt{-1})$, where x 6. (3) $R = \left[-\frac{1}{2}, \frac{1}{2} \right]$ (4) R = [-1, 1]and y are real numbers, then y - x equals : (1) - 85(2) 85 Ans. (2) (3) - 91(4) 91 **Sol.** f(0) = 0 & f(x) is odd. Ans. (4) Further, if x > 0 then **Sol.** $\left(-2-\frac{i}{2}\right)^3 = -\frac{(6+i)^3}{27}$ $f(\mathbf{x}) = \frac{1}{\mathbf{x} + \frac{1}{2}} \in \left(0, \frac{1}{2}\right]$ $=\frac{-198-107i}{27}=\frac{x+iy}{27}$ Hence, $f(\mathbf{x}) \in \left| -\frac{1}{2}, \frac{1}{2} \right|$ Hence, y - x = 198 - 107 = 912

9.	The sum of the real values of x for which the middle term in the binomial expansion of 1					
	$\left(\frac{x^3}{3} + \frac{3}{x}\right)$	\int^{8} equals 50	570 is :			
	(1) 6	(2) 8	(3) 0	(4) 4		
Ans.	(3)					
Sol.	$T_5 = {}^8C_4$	$\frac{x^{12}}{81} \times \frac{81}{x^4} = 5$	5670			
	$\Rightarrow 70x^8 =$	= 5670			An	
	$\Rightarrow x = +$	$\sqrt{3}$			AII	
10	The value	e of r for w	hich		Sol	
10.	$^{20}C_{20}C_{0} = -$	$+ {}^{20}C_{-1} {}^{20}C_{1} -$	$+ {}^{20}C_{-2} {}^{20}C_{2}$	$+ \dots {}^{20}C_{0}{}^{20}C_{0}$		
	is maxim	um, is	$\sigma_{r-2} \sigma_2$			
	(1) 20		(2) 15			
	(3) 11		(4) 10			
Ans.	(1)				S	
Sol.	Given sum = coefficient of x^r in the expansion of $(1 + x)^{20}(1 + x)^{20}$,					
	which is	equal to ⁴⁰ C	r	$\mathbf{\lambda}$		
	It is maxi	imum when	r = 20	. X `		
11.	Let a_1, a_2	,, a ₁₀ be	a G.P. If $\frac{a}{a}$	$\frac{1_3}{1_1} = 25$, then		
	$\frac{a_9}{a_5}$ equals :					
	(1) $2(5^2)$		$(2) 4(5^2)$)		
	(3) 54		$(4) 5^3$			
Ans.	(3)					
Sol.	a ₁ , a ₂ ,, a ₁₀ are in G.P.,					
	Let the c	ommon ratio	b be r			
	$\frac{a_3}{a_1} = 25 \implies \frac{a_1 r^2}{a_1} = 25 \implies r^2 = 25$					
	$\frac{a_9}{a_5} = \frac{a_1 r^8}{a_1 r^4} = r^4 = 5^4$					

2. If
$$\int \frac{\sqrt{1-x^2}}{x^4} dx = A(x) \left(\sqrt{1-x^2}\right)^m + C$$
, for
a suitable chosen integer m and a function

a suitable chosen integer m and a function A(x), where C is a constant of integration then $(A(x))^m$ equals :

(1)
$$\frac{-1}{3x^3}$$
 (2) $\frac{-1}{27x^9}$
(3) $\frac{1}{9x^4}$ (4) $\frac{1}{27x^6}$
Ans. (2)
Sol. $\int \frac{\sqrt{1-x^2}}{x^4} dx = A(x)(\sqrt{1-x^2})^m + C$
 $\int \frac{|x|}{x^2} \sqrt{\frac{1}{x^2} - 1} dx$,
 $Put \frac{1}{x^2} - 1 = t \Rightarrow \frac{dt}{dx} = \frac{-2}{x^3}$
Case-1 $x \ge 0$
 $-\frac{1}{2}\int \sqrt{t} dt \Rightarrow -\frac{t^{3/2}}{3} + C$
 $\Rightarrow -\frac{1}{3}\left(\frac{1}{x^2} - 1\right)^{3/2}$
 $\Rightarrow \frac{(\sqrt{1-x^2})^3}{-3x^2} + C$
 $A(x) = -\frac{1}{3x^3} \text{ and } m = 3$
 $(A(x))^m = \left(-\frac{1}{3x^3}\right)^3 = -\frac{1}{27x^9}$
Case-II $x \le 0$
We get $\frac{(\sqrt{1-x^2})^3}{-3x^3} + C$
 $A(x) = \frac{1}{-3x^3}, m = 3$
 $(A(x))^m = \frac{-1}{27x^9}$

3

13. In a triangle, the sum of lengths of two sides is x and the product of the lengths of the same two sides is y. If $x^2 - c^2 = y$, where c is the length of the third side of the triangle, then the circumradius of the triangle is :

(1)
$$\frac{y}{\sqrt{3}}$$
 (2) $\frac{c}{\sqrt{3}}$ (3) $\frac{c}{3}$ (4) $\frac{3}{2}y$

Ans. (2)

Sol. Given a + b = x and ab = yIf $x^2 - c^2 = y \implies (a + b)^2 - c^2 = ab$ $\Rightarrow a^2 + b^2 - c^2 = -ab$ $\Rightarrow \frac{a^2 + b^2 - c^2}{2ab} = -\frac{1}{2}$ $\Rightarrow \cos C = -\frac{1}{2}$ $\Rightarrow \angle C = \frac{2\pi}{3}$ $R = \frac{c}{2 \sin C} = \frac{c}{\sqrt{3}}$

 $\frac{\sin^2 x}{\lceil \underline{x} \rceil}$ The value of the integral 14.

> (where [x] denotes the greatest integer less than 20 Cr or equal to x) is : 2) 4 – sin4

(1) 4

Ans. (4)

Sol.
$$I = \int_{-2}^{-2} \frac{st}{\left[\frac{x}{\pi}\right]}$$

$$I = \int_{0}^{2} \left(\frac{\sin^{2} x}{\left[\frac{x}{\pi}\right] + \frac{1}{2}} + \frac{\sin^{2}(-x)}{\left[-\frac{x}{\pi}\right] + \frac{1}{2}} \right) dx$$
$$\left(\left[\frac{x}{\pi}\right] + \left[-\frac{x}{\pi}\right] = -1 \text{ as } x \neq n\pi \right)$$
$$I = \int_{0}^{2} \left(\frac{\sin^{2} x}{\left[\frac{x}{\pi}\right] + \frac{1}{2}} + \frac{\sin^{2} x}{-1 - \left[\frac{x}{\pi}\right] + \frac{1}{2}} \right) dx = 0$$

If the system of linear equations 15. $2\mathbf{x} + 2\mathbf{y} + 3\mathbf{z} = \mathbf{a}$ 3x - y + 5z = bx - 3y + 2z = cwhere a, b, c are non-zero real numbers, has more then one solution, then : (1) b - c - a = 0(2) a + b + c = 0(3) b + c - a = 0(4) b - c + a = 0Ans. (1)**Sol.** $P_1: 2x + 2y + 3z = a$ $\mathbf{P}_2: \mathbf{3x} - \mathbf{y} + \mathbf{5z} = \mathbf{b}$ $P_3 : x - 3y + 2z = c$ We find $P_1 + P_3 = P_2 \Longrightarrow a + c =$ A square is inscribed in he circle 16. $x^2 + y^2 - 6x + 8y - 103 = 0$ with its sides parallel to the corrdinate axes. Then the distance of the vertex of this square which is nearest to the origin is :-(2) $\sqrt{137}$ (1) 13(4) $\sqrt{41}$ (3) 6(4) $R = \sqrt{9 + 16 + 103} = 8\sqrt{2}$ Sol. OA = 13C(11,4) $OB = \sqrt{265}$ $OC = \sqrt{137}$ B (11,–12) $OD = \sqrt{41}$ 17. Let $f_k(x) = \frac{1}{k} (\sin^k x + \cos^k x)$ for k = 1, 2,3, Then for all $x \in R$, the value of $f_4(x) - f_6(x)$ is equal to :-(1) $\frac{5}{12}$ (2) $\frac{-1}{12}$ (3) $\frac{1}{4}$ (4) $\frac{1}{12}$ Ans. (4) **Sol.** $f_4(x) - f_6(x)$ $=\frac{1}{4}(\sin^4 x + \cos^4 x) - \frac{1}{6}(\sin^6 x + \cos^6 x)$ $=\frac{1}{4}\left(1-\frac{1}{2}\sin^2 2x\right)-\frac{1}{6}\left(1-\frac{3}{4}\sin^2 2x\right)=\frac{1}{12}$

18. Let [x] denote the greatest integer less than or equal to x. Then :-

$$\lim_{x \to 0} \frac{\tan(\pi \sin^2 x) + (|x| - \sin(x[x]))^2}{x^2}$$
(1) equals π

- (2) equals 0
- (3) equals $\pi + 1$
- (4) does not exist

Ans. (4)

Sol. R.H.L.
$$= \lim_{x \to 0^+} \frac{\tan(\pi \sin^2 x) + (|x| - \sin(x[x]))^2}{x^2}$$

(as $x \to 0^+ \Rightarrow [x] = 0$)
 $= \lim_{x \to 0^+} \frac{\tan(\pi \sin^2 x) + x^2}{x^2}$
 $= \lim_{x \to 0^+} \frac{\tan(\pi \sin^2 x)}{(\pi \sin^2 x)} + 1 = \pi + 1$
L.H.L. $= \lim_{x \to 0^-} \frac{\tan(\pi \sin^2 x) + (-x + \sin x)^2}{x^2}$
(as $x \to 0^- \Rightarrow [x] = -1$)
 $\lim_{x \to 0^+} \frac{\tan(\pi \sin^2 x)}{\pi \sin^2 x} \cdot \frac{\pi \sin^2 x}{x^2} + (-1 + \frac{\sin x}{x})^2 \Rightarrow \pi$
R.H.L. \neq L.H.L.

19. The direction ratios of normal to the plane through the points (0, -1, 0) and (0, 0, 1) and making an anlge π/4 with the plane y-z+5=0 are:

(1) $2\sqrt{3}$, 1, -1 (2) 2, $\sqrt{2}$, $-\sqrt{2}$

- $(2) 2, \sqrt{2}, -\sqrt{2}$
- (3) 2, -1, 1
- (4) $\sqrt{2}$, 1, -1

Ans. (2, 4)

Sol. Let the equation of plane be a(x - 0) + b(y + 1) + c(z - 0) = 0It passes through (0,0,1) then $b + c = 0 \qquad \dots(1)$ Now $\cos \frac{\pi}{4} = \frac{a(0) + b(1) + c(-1)}{\sqrt{2}\sqrt{a^2 + b^2 + c^2}}$ $\Rightarrow a^2 = -2bc \text{ and } b = -c$ we get $a^2 = 2c^2$ $\Rightarrow a = \pm\sqrt{2}c$ $\Rightarrow \text{ direction ratio } (a, b, c) = (\sqrt{2}, -1, 1) \text{ or } (\sqrt{2}, 1, -1)$ 20. If $x \log_e(\log_e x) - x^2 + y^2 = 4(y > 0)$, then dy/dx at x = e is equal to :

(1)
$$\frac{e}{\sqrt{4 + e^2}}$$

(2) $\frac{(1+2e)}{2\sqrt{4 + e^2}}$
(3) $\frac{(2e-1)}{2\sqrt{4 + e^2}}$
(4) $\frac{(1+2e)}{\sqrt{4 + e^2}}$

Ans. (3)

Sol. Differentiating with respect to x,

$$x.\frac{1}{\ln x}\cdot\frac{1}{x} + \ln(\ln x) - 2x + 2y.\frac{dy}{dx} = 0$$

at $x = e$ we get
$$1 - 2e + 2y\frac{dy}{dx} = 0 \implies \frac{dy}{dx} = \frac{2e - 1}{2y}$$
$$\implies \frac{dy}{dx} = \frac{2e - 1}{2\sqrt{4 + e^2}} \text{ as } y(e) = \sqrt{4 + e^2}$$

21. The straight line x + 2y = 1 meets the coordinate axes at A and B. A circle is drawn through A, B and the origin. Then the sum of perpendicular distances from A and B on the tangent to the circle at the origin is :

$$(1) \frac{\sqrt{5}}{4} \sqrt{5}$$

(2)
$$\frac{\sqrt{3}}{2}$$

- (3) $2\sqrt{5}$
- (4) $4\sqrt{5}$
- Ans. (2)



Equation of circle

$$(x - 1)(x - 0) + (y - 0) \bigg(y -$$

 $\Rightarrow x^2 + y^2 - x - \frac{y}{2} = 0$

Equation of tangent of origin is $2x + \ell_1 + \ell_2 = \frac{2}{\sqrt{2}} + \frac{1}{\sqrt{2}}$

 $\frac{1}{2}$

= 0

$$\ell_1 + \ell_2 = \frac{1}{\sqrt{5}} + \frac{1}{2\sqrt{5}}$$
$$= \frac{4+1}{2\sqrt{5}} = \frac{\sqrt{5}}{2}$$

- **22.** If q is false and $p \land q \leftrightarrow r$ is true, then which one of the following statements is a tautology?
 - (1) $(p \lor r) \rightarrow (p \land r)$
 - (2) p v r
 - (3) p ^ r

$$(4)(p \land r) \to (p \lor r)$$

Ans. (4)

Sol. Given q is F and $(p \land q) \leftrightarrow r$ is T $\Rightarrow p \land q$ is F which implies that r is F $\Rightarrow q$ is F and r is F $\Rightarrow (p \land r)$ is always F $\Rightarrow (p \land r) \rightarrow (p \lor r)$ is tautology. **23.** If y(x) is the solution of the differential equation

$$\frac{dy}{dx} + \left(\frac{2x+1}{x}\right)y = e^{-2x}, x > 0,$$
where $y(1) = \frac{1}{2}e^{-2}$, then :
(1) $y(x)$ is decreasing in $(0, 1)$
(2) $y(x)$ is decreasing in $\left(\frac{1}{2}, 1\right)$
(3) $y(\log_e 2) = \frac{\log_e 2}{4}$
(4) $y(\log_e 2) = \log_e 4$
Ans. (2)
Sol. $\frac{dy}{dx} + \left(\frac{2x+1}{x}\right)y = e^{-2x}$
 $FF. = e^{\int \left(\frac{2x+1}{x}\right)dx} = e^{\int \left(2+\frac{1}{x}\right)dx} = e^{2x+6nx} = e^{2x}.x$
So, $y(xe^{2x}) = \int e^{-2x}.xe^{2x} + C$
 $\Rightarrow xye^{2x} = \int x \, dx + C$
 $\Rightarrow 2xye^{2x} = x^2 + 2C$
It passess through $\left(1, \frac{1}{2}e^{-2}\right)$ we get $C = 0$
 $y = \frac{xe^{-2x}}{2}$
 $\Rightarrow \frac{dy}{dx} = \frac{1}{2}e^{-2x}(-2x+1)$
 $\Rightarrow f(x)$ is decreasing in $\left(\frac{1}{2}, 1\right)$
 $y(\log_e 2) = \frac{(\log_e 2)e^{-2(\log_e 2)}}{2}$
 $= \frac{1}{8}\log_e 2$

24. The maximum value of the function $f(x) = 3x^3 - 18x^2 + 27x - 40$ on the set $S = \{x \in R : x^2 + 30 \le 11x\}$ is : (1) 122(2) - 222(3) - 122(4) 222 Ans. (1) **Sol.** S = {x \in R, x² + 30 - 11x \leq 0} $= \{ x \in \mathbf{R}, 5 \le x \le 6 \}$ Now $f(x) = 3x^3 - 18x^2 + 27x - 40$ $\Rightarrow f'(\mathbf{x}) = 9(\mathbf{x} - 1)(\mathbf{x} - 3),$ which is positive in [5, 6] \Rightarrow f(x) increasing in [5, 6] Hence maximum value = f(6) = 122If one real root of the quadratic equation 25. $81x^2 + kx + 256 = 0$ is cube of the other root, then a value of k is (1) - 81(2) 100(3) - 300(4) 144Ans. (3) **Sol.** $81x^2 + kx + 256 = 0$; $x = \alpha, \alpha^3$ $\Rightarrow \alpha^4 = \frac{256}{81} \Rightarrow \alpha = \pm \frac{4}{3}$ Now $-\frac{k}{81} = \alpha + \alpha^3 = \pm \frac{100}{27}$ \Rightarrow k = ±300 Two circles with equal radii are intersecting at 26. the points (0, 1) and (0, -1). The tangent at the point (0, 1) to one of the circles passes through the centre of the other circle. Then the distance between the centres of these circles is : (1) 1(3) $2\sqrt{2}$ Ans. (4) Sol. In $\triangle APO$ $\left(\frac{\sqrt{2} r}{2}\right)^2 + 1^2 = r^2$ $\Rightarrow r = \sqrt{2}$ So distance between centres = $\sqrt{2} r = 2$

27. Equation of a common tangent to the parabola y² = 4x and the hyperbole xy = 2 is :
(1) x + 2y + 4 = 0
(2) x - 2y + 4 = 0
(3) x + y + 1 = 0
(4) 4x + 2y + 1 = 0

Ans. (1)

Sol. Let the equation of tangent to parabola

$$y^2 = 4x \text{ be } y = mx + \frac{1}{m}$$

It is also a tangent to hyperbola xy = 2

$$\Rightarrow x\left(mx + \frac{1}{m}\right) = 2$$
$$\Rightarrow x^{2}m + \frac{x}{m} - 2 = 0$$
$$D = 0 \Rightarrow m = -\frac{1}{2}$$

So tangent is 2y + x + 4 = 0

The plane containing the line $\frac{x-3}{2} = \frac{y+2}{-1} = \frac{z-1}{3}$

and also containing its projection on the plane

2x + 3y - z = 5, contains which one of the following points ?

Ans. (1)

Sol. The normal vector of required plane

$$= (2\hat{i} - \hat{j} + 3\hat{k}) \times (2\hat{i} + 3\hat{j} - \hat{k})$$
$$= -8\hat{i} + 8\hat{j} + 8\hat{k}$$

So, direction ratio of normal is (-1, 1, 1)So required plane is -(x - 3) + (y + 2) + (z - 1) = 0 $\Rightarrow -x + y + z + 4 = 0$

Which is satisfied by (2, 0, -2)

29. If tangents are drawn to the ellipse $x^2 + 2y^2 = 2$ at all points on the ellipse other than its four vertices then the mid points of the tangents intercepted betwen the coordinate axes lie on the curve :

(1)
$$\frac{x^2}{2} + \frac{y^2}{4} = 1$$
 (2) $\frac{x^2}{4} + \frac{y^2}{2} = 1$
(3) $\frac{1}{2x^2} + \frac{1}{4y^2} = 1$ (4) $\frac{1}{4x^2} + \frac{1}{2y^2} = 1$

Ans. (3)

Sol. Equation of general tangent on ellipse

$$\frac{x}{a \sec \theta} + \frac{y}{b \csc \theta} = 1$$
$$a = \sqrt{2}, b = 1$$
$$\Rightarrow \frac{x}{\sqrt{2} \sec \theta} + \frac{y}{\csc \theta} = 1$$

Let the midpoint be (h, k)

$$h = \frac{\sqrt{2} \sec \theta}{2} \implies \cos \theta = \frac{1}{\sqrt{2}h}$$

and $k = \frac{\csc \theta}{2} \implies \sin \theta = \frac{1}{2k}$
 $\therefore \sin^2 \theta + \cos^2 \theta = 1$
 $\implies \frac{1}{2h^2} + \frac{1}{4k^2} = 1$
 $\implies \frac{1}{2x^2} + \frac{1}{4y^2} = 1$

30. Two integers are selected at random from the set {1, 2,..., 11}. Given that the sum of selected numbers is even, the conditional probability that both the numbers are even is :



Sol. Since sum of two numbers is even so either both are odd or both are even. Hence number of elements in reduced samples space

$$= {}^{5}C_{2} + {}^{6}C_{2}$$

so required probability =
$$\frac{{}^{5}C_{2}}{{}^{5}C_{2} + {}^{6}C_{2}}$$